



## Verifiable multi-authority attribute based encryption scheme with different permissions

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### ABSTRACT

*In this paper, we study the traffic information granular computing theory and build traffic information fusion model, framework and implementation program based on granular computing. We raise uncertainty reduction algorithms for traffic flow prediction and congestion recognition algorithms based on granular computing theory, which will provide new ideas and methods in the complex decision making under uncertainty problems of the transportation systems. In an attribute based encryption scheme, each user is identified by a set of attributes, which are used to determine encryption ability for each ciphertext. On the base of attribute based encryption and symmetric encryption algorithm, it proposes a verifiable multi-authority attribute based encryption scheme. In our scheme, access control permission is divided into two kinds: Read and Write for the first time. An encryptor can easily deal with this problem by using two different secret keys. When a user wants to get Read permission, he just needs to go to some authorities, yet not all. We also provide a verification scheme that ensures the integrity of data and realness of data sources. The encryptor generates a signature while encryption, the user carries out verification with given signature and the decrypted message. The scheme not only enhances the confidentiality of data, but also supports more flexible and more fine-grained access control strategy.*

**Key words:** Multiple authorities, Attribute based encryption, Identity based encryption, Permission, Pseudorandom function (PRF)

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### INTRODUCTION

In 2005, Sahai and Waters introduced Fuzzy Identity-based Encryption (Fuzzy-IBE) firstly [1]. In the scheme, the identity of user was described as a set of attribute, while the matching relation of identity was transitioned from the original "match" into "similarity matching". In 2006, Fuzzy-IBE is extended to the attribute based encryption (ABE) by Goyal, Sahai and Waters et al. [2], they also expounded the concept and significance of attribute based encryption. In attribute based encryption mechanism, the user identity information was generalized as related attributes, and they divided ABE scheme into two types: Ciphertext-Policy ABE (CP-ABE) and Key-Policy ABE (KP-ABE) based on different applications.

With some basic schemes [3,4,5] proposed, researchers put forward the deep research work and research direction on attribute cryptography. Emura [6] and Chen et al. [7] considered the "and" gate access structure. Attrapadung and Libert [8] constructed an ABE scheme supporting general access structure. The length of ciphertext and the encryption or decryption cost was constant in this scheme. Based on the LWE problem, Agrawal et al. [9] has presented a new ABE scheme, in which access policy was threshold, it also discussed the difficulty of general access structure based on lattice. Maji et al. [10] first presented the concept and safety definition on attribute based signature (ABS). In ABS, the signer generates a signature when given a message and a policy, the verifier can ensure whether the signature has been generated by the user who satisfying attribute policy. Ateniese et al. [11] first proposed an attribute based secret

handshakes scheme, which opened the research of attribute based security protocol. Chase et al. [12,13] solved a single authority corrupted problem by employing multiple authorities, and prevent the collusion between users by adopting a global identity GID for each user. Lewko et al. [14] present another multi-authority scheme, in which any party can become an authority and does not require any "central authority".

Attribute based encryption has been rapidly developed since it was born, and it is a hot direction in cryptography recently, which realizes non-interactive fine-grained access control mechanism, expands one-to-one model to one-to-many model on encryption and decryption, greatly enriches the flexibility of encryption policy and description of user permissions. Hence, it has a good application prospect in distributed file management, third party data storage, pay TV system and other fields [15,16].

However, in all existing ABE schemes, all users can only get one same kind of permission if satisfying access policy. With the rapid development of network, the rise of cloud computing and different demand growth of large-scale user, it is necessary to give users different permissions. For example: there are four attribute authorities monitoring four attribute sets  $A_1 = \{a_1, a_2, a_3\}$ ,  $A_2 = \{a_4, a_5\}$ ,  $A_3 = \{a_6, a_7, a_8\}$ ,  $A_4 = \{a_9, a_{10}, a_{11}, a_{12}\}$ , the minimal requirements are  $d_1 = 2$ ,  $d_2 = 1$ ,  $d_3 = 2$ ,  $d_4 = 2$ .  $u_1, u_2, u_3$  are three users and  $C_1, C_2, C_3$  are ciphertexts, the related attribute sets are  $A_{u_1} = \{a_1, a_2, a_4, a_6, a_8, a_9, a_{10}\}$ ,  $A_{u_2} = \{a_1, a_4, a_7, a_8\}$ ,  $A_{u_3} = \{a_1, a_2, a_4, a_7, a_8, a_{10}, a_{12}\}$ ,  $A_{C_1} = \{a_1, a_2, a_4, a_6, a_7, a_8\}$ ,  $A_{C_2} = \{a_6, a_8, a_9, a_{10}\}$ ,  $A_{C_3} = \{\{a_1, a_2, a_4, a_6, a_8\}, \{a_1, a_2, a_4, a_6, a_8, a_{10}, a_{11}, a_{12}\}\}$ .

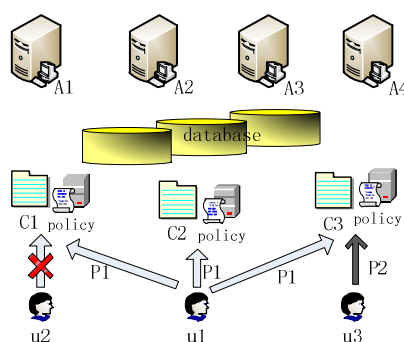


Fig. 1: More Fine-grained Access control From ABE

In Fig 1, 1)  $u_1$  can decrypt  $C_1$ , while  $u_2$  can't. And  $u_1$  only goes to attribute authority  $A_1, A_2$  and  $A_3$ , not to  $A_4$ ; 2)  $u_1$  can decrypt  $C_1$  and  $C_2$ , but referring different authorities set  $\{A_1, A_2, A_3\}$  and  $\{A_3, A_4\}$ , the number of authorities is different, too; 3)  $u_1$  gets  $P_1$  permission by going to  $\{A_1, A_2, A_3\}$ , but  $u_3$  gets  $P_2$  permission by going to all authorities.

From the example, we can see that: 1) in different applications, there are many permissions, such as *Read*, *Copy*, *Reference* and *Write*. Therefore, permission problem should be considered while designing access control policy. The basic operation of user is *Read* or *Write*. Of course, one also has *Read* permission if he has *Write* permission; 2) a user can get one permission while only going to some authorities. We also provide a verification scheme by a signature. Hence, in this paper, in order to present *Read* Permission and *Write* Permission, we select two different keys to control the two permissions, and the access policy is generated by an encryptor.

The remainder of this paper is organized as follows: We discuss the novelty and contributions of this paper in Section II. In Section III, definitions and preliminaries are presented. In Section IV, the proposed verifiable multi-authority attribute based encryption scheme with different permission is presented, and the security analysis of the proposed scheme is discussed. In Section V, performance discussion is presented. Finally, conclusions and possible future research directions are presented in Section VI.

## OUR CONTRIBUTIONS

The object of our proposal is to present a verifiable multi-authority ABE Scheme and resolve following problems:

- Many scholars have applied ABE to access control, but the issue of different permissions in one system has been ignored. For example, some users can read, others can copy.
- In the previous multi-authority schemes, the user must satisfy the attributes requirement of each authority to get decryption ability. It is to say that the user must go to all authorities. The author of [12] referred the problem in extensions, but there was some limit, which will be discussed in detail in section V.B.
- In existing attribute based encryption scheme, the attention is focused on decryptor, while the honesty of encryptor and the integrity of data are ignored. For example, a user meeting the attribute requirement got a message while the message has been corrupted before encrypted.

To overcome these problems, we propose a verifiable multi-authority attribute based encryption scheme with different permissions. This scheme works as follows: First, the central authority setup the system parameters, and all authorities generate public keys and secret keys for user  $u$ . Second, a sender encrypts a message  $M$  with a symmetric key  $K_{read}$ , which only provides Read permission. Then  $K_{read}$  and Write permission  $K_{write}$  are encrypted respectively. In the process the encryptor generates access control policy for users and generates a signature on  $M$ . Third, the user gets Read permission and  $M$ , just meeting some authorities requirement, or even one. After, the user can verify the integrity of  $M$  and authenticity of the encryptor by offered signature. Moreover, if the user wants to obtain Write permission, he should meet all attribute requirements of all authorities including the central authority.

The contributions of this paper are as follows:

- In the scheme, we realize the permission distinguish that let user get Read Permission or Write Permission based on having attributes. The access control policy is generated by the encryptor, so the encryptor has more choice rights, which is more friendly to users. On the premise of the protection of data confidentiality, the scheme provides different permissions for users having different attributes.
- To obtain Read permission, just some authority are involved, even only one. This scheme avoids the shortcomings that one must go to all attribute authorities.
- There generates a BLS short signature [17] for message  $M$  while encryption to present verification, which ensures the confidentiality, integrity of data and non-repudiation of encryptor.

## PRELIMINARY

In our ABE scheme, we assume that: 1) there are  $K$  attribute authorities and a trusted central authority. 2) the universe of attributes can be partitioned into  $K$  attribute sets. Each attribute authority will monitor one attribute set while the central authority will not monitor any attributes. The notations referred in the paper will be shown in Table I.

Table.1 Notation

Item	Description
$A_u$	the attribute set of user $u$
$A_C$	the attribute set of a ciphertext
$A_u^k$	attributes of $u$ handled by authority $k$
$A_C^k$	attributes of ciphertext handled by authority $k$
GID	the global identity of each $u$
$d_k$	the required minimum number of $ A_u^k \cap A_C^k $

## A. BILINEAR MAPS AND COMPLEXITY ASSUMPTION

Let  $G_1$  and  $G_2$  be two cyclic multiplicative groups of the same large prime order  $p$ .

**Definition 1 (Bilinear Maps)** A bilinear pairing is a computable bilinear map between two groups  $e: G_1 \times G_1 \rightarrow G_2$ . It is the modified Weil pairing or Tate pairing which has the following properties:

- 1). *Bilinear*: For any  $g^a, g^b \in G_1$ ,  $e(g^a, g^b) = e(g, g)^{ab}$  ;
- 2). *Non-degenerate*: There exists  $P, Q \in G_1$ , such that  $e(P, Q) \neq 1$  ;
- 3). *Efficient*: There exists an efficient algorithm to compute the map.

**Definition 2 (Decisional Bilinear Diffie-Hellman (BDH) Assumption)** Suppose a challenge chooses  $a, b, c, R$  from  $Z_p^*$  randomly. The decisional BDH Assumption is that no polynomial-time adversary is to be able to distinguish the

tuple  $\langle g, g^a, g^b, g^c, e(g, g)^{abc} \rangle$  from the tuple  $\langle g, g^a, g^b, g^c, e(g, g)^R \rangle$  with more than a negligible advantage.

**Definition 3 (Decisional Modified Bilinear Diffie-Hellman (MBDH) Assumption)** Suppose a challenger chooses  $a, b, c, R$  from  $\mathbf{Z}_p^*$  randomly. The decisional MBDH Assumption is that no polynomial-time adversary is to be able to distinguish the tuple  $\langle g, g^a, g^b, g^c, e(g, g)^{abc} \rangle$  from the tuple  $\langle g, g^a, g^b, g^c, e(g, g)^R \rangle$  with more than a negligible advantage.

### B. VERIFIABLE MULTI-AUTHORITY ABE SCHEME WITH DIFFERENT PERMISSIONS (VMA-ABE-DP)

The proposed scheme of verifiable multi-authority ABE scheme with different permissions consisting of four phases: **Setup**, **KeyGen**, **EncSig** and **DecVer**, are shown as follows.

- **Setup**: Given a security parameter, the trusted central authority runs a randomized algorithm which outputs a public key, secret key pair for each of the attribute authorities, and also outputs a system public key and master secret key for himself.
- **KeyGen**: In this phase, there are two types of key: Attribute Key Generation and Central key Generation.
  - **Attribute Key Generation**: A randomized algorithm run by an attribute authority. Takes as input the authority's secret key, the authority's value  $d_k$ , a user's **GID**, and a set of attributes in the authority's domain. Outputs secret key for the user.
  - **Central Key Generation**: A randomized algorithm run by the central authority. Input the master secret key and a user's **GID**, then output secret key for the user.
- **EncSig**: The sender carries out two work: Encrypt and Signature
  - **Encryption**: A randomized algorithm run by an encryptor. Input a set of attributes for some or all authorities, a message, and the system public key. Output ciphertext.
  - **Signature**: A randomized algorithm run by an encryptor. Input a message and the signature key. Output signature.
- **DecVer**: The user carries out two work: Decrypt and Verification
  - **Decryption**: A deterministic algorithm run by a user. Takes as input a ciphertext, which is encrypted under attribute set  $A_C$  and decryption keys for an attribute set  $A_u$ . Outputs a message  $M$  if  $|A_C^k \cap A_u^k| \geq d_k$  for a certain number of authorities or all authorities  $k$ .
  - **Verification**: A verification algorithm run by a user. Takes as input a signature, the system public key and the decrypted  $M$ . Outputs *Yes* or *No*.

### C. SECURITY MODEL

To prove confidentiality of the proposed scheme, consider the selective identity (sid) attack model, the prototype scheme is selective identity security model in [1, 12]. The game is followed.

- **Setup**
  - The adversary sends a list of attribute sets  $A_C = A_C^1 \cdots A_C^l, l \leq K$ , one for each authority. He also sends a list of corrupted authorities which cannot include the central authority.
  - The challenger generates parameters for the system and sends to the adversary. This means the system public key, public keys for all honest authorities, and secret keys for all corrupted authorities.
- **Queries**: The adversary can make as many secret key queries as he wants to the attribute authorities or to the central authority. The only requirements are same as in [12].
- **Challenge**: The adversary sends two messages  $M_0$  and  $M_1$ . The challenger chooses a bit  $b$ , computes the encryption of  $M_b$  under symmetric key which is encrypted for attribute set  $A_C$ , and sends these ciphertexts to the adversary.

- **More Queries:** The adversary may make more secret key queries subject to the requirements described above.
- **Guess:** The adversary outputs a guess  $b'$

The adversary is said to succeed if  $b = b'$ .

**Definition 4 (Selective ID Secure)** The verifiable multi-authority attribute scheme with different permissions is secure if there exists a negligible function  $\nu$  such that, in above game any adversary will succeed with probability at most  $\frac{1}{2} + \nu(k)$ .

#### D. BLS SIGNATURE

The signature scheme comprises three algorithms, **KeyGen**, **Sign**, and **Verify**. It makes use of a full-domain hash function  $H : \{0,1\}^* \rightarrow G_1$ .

**KeyGen:** Pick  $x \in_R \mathbb{Z}_p^*$ , compute  $PK = g^x$ . The public key is  $PK$ , the secret key is  $x$ .

**Sign:** Given the secret key  $x$  and a message  $M$ , compute  $h = H(M)$  and  $\sigma = h^x$ . The signature is  $\sigma$ .

**Verify:** Given a public key  $PK$ , a message  $M$  and a signature  $\sigma$ , compute  $h = H(M)$ . Then verify  $e(g, \sigma) = e(PK, h)$ .

#### VERIFIABLE MULTI-AUTHORITY ATTRIBUTE BASED ENCRYPTION SCHEME WITH DIFFERENT PERMISSIONS (VMA-ABE-DP)

We now present our verifiable multi-authority attribute based encryption scheme with different permissions. We use mixed encryption mechanism, where a symmetric key  $K_{read}$  is used to encrypt a message, then  $K_{read}$  and  $K_{write}$  are encrypted with the public key cryptosystem. In order to prevent collusion, the scheme uses the global identity **GID** for each user, and which is tied with his attributes and his public key. There is also a BLS short signature to monitor the encryptor.

#### A. CONSTRUCTION

The proposed verifiable multi-authority attribute based encryption scheme with different permissions vMA-ABE-DP, consisting of four phases: **Setup**, **KeyGen**, **EncSig** and **DecVer**, are shown as follows.

- **Setup:** Let  $G_1, G_2$  be two cyclic group of prime order  $p$  and generator  $g \in G_1$ ,  $e : G_1 \times G_1 \rightarrow G_2$ . Select seeds  $s_1, \dots, s_K$  for all authorities. Also select  $y_0, \{t_{k,i}\}_{k=1, \dots, K; i=1, \dots, n}$  from  $\mathbb{Z}_q$ .  $H$  is a hash function,  $H : \{0,1\}^* \rightarrow G_1$ .

**System Public Key** is  $Y_0 = e(g, g)^{y_0}$ .

- **KeyGen:**

- **Attribute Authority  $k$**

**Authority Secret Key**  $s_k, t_{k,1}, \dots, t_{k,n}$

**Authority Public Key**  $T_{k,1}, \dots, T_{k,n}$  where  $T_{k,i} = g^{t_{k,i}}$ ,  $Y_{k,u} = e(g, g)^{y_{k,u}}$ .

**Authority Key for User  $u$**  Let  $y_{k,u} = F_{s_k}(u)$ . Select random  $d_k - 1$  degree polynomial  $p$  with

$p(0) = y_{k,u}$ . Secret key:  $\{D_{k,i} = g^{\frac{p(i)}{t_{k,i}}}\}_{i \in A_u}$ .

- **Central Authority  $k$**

**Central Authority Secret Key**  $y_0$

**Secret Key for User  $u$**  Let  $y_{k,u} = F_{s_k}(u)$ . Secret key:  $D_{CA} = g^{(y_0 - \sum_{k=0}^K y_{k,u})}$ .

• **EncSig:**The user whose identifier is **GID**, randomly selects  $s \in_R \mathbf{Z}_q, P_u = g^s, \{E_{k,i} = T_{k,i}^s\}_{i \in A_u, \forall k}$ .  $M$  is a message with a symmetric key  $K_{read}$  (such as AES), which control *ReadPermission*, and *WritePermission* key:  $K_{write}$ .

-**Encryption:**  $C_r = E_{K_{read}}(M), E = Y_0 K_{write}$ . The user generates a set  $LEB = \{k \mid A_C \cap A_u \geq d_k\}$  and  $K_{read}$  is partitioned into  $|LEB|$  parts:  $K_{r1}, \dots, K_{r|LEB|}$ , where  $K_{read} = K_{r1} \parallel \dots \parallel K_{r|LEB|}$ . Then  $\{EE_k = Y_{k,u}^s K_{rk}\}_{k \in LEB}$ .

-**Signature:** Compute  $h = H(M)$  and  $\sigma = h^s$ . The signature is  $\sigma$ .

The ciphertext is:

$$C = \langle C_r, E, P_u, \{E_{k,i}\}_{i \in A_u, \forall k}, \{EE_k\}_{k \in LEB}, \sigma \rangle.$$

• **DecVer:**

-**Compute  $K_{read}$ :** For each authority  $k \in LEB$ , for  $d_k$  attributes  $i \in A_C^k \cap A_u^k$ , compute  $e(E_{k,i}, D_{k,i}) = e(g, g)^{p(i)s}$ . Interpolate to find  $Y_{k,u}^s = \prod e(g, g)^{p(i)s \Delta_{i,s}(0)} = e(g, g)^{p(0)s} = e(g, g)^{y_{k,u}^s}$ , then compute  $\{K_{rk} = EE_k / Y_{k,u}^s\}_{k \in LEB}$  to get  $K_{read} = K_{r1} \parallel \dots \parallel K_{r|LEB|}$ , so

$$M' = D_{K_{read}}(C_r) \tag{1}$$

-**Verification:** First, the user computes  $h = H(M)$ . Then verifies

$$e(g, \sigma) = e(P_u, h) \tag{2}$$

If (2) is established,  $M$  and the encryptor are not corrupted; else,  $M$  is corrupted or the signer is not the right one.

-**Compute  $K_{write}$ :** For each authority  $k$  and  $d_k$  attributes  $i \in A_C^k \cap A_u^k$ , compute  $e(E_{k,i}, D_{k,i}) = e(g, g)^{p(i)s}$ . Interpolate to find  $Y_{k,u}^s = e(g, g)^{p(0)s} = e(g, g)^{y_{k,u}^s}$  for each  $k$ . Compute  $Y_{CA}^s = e(E_{CA}, D_{CA})$ , combine these values to obtain  $Y_{CA}^s \prod_{k=1}^K Y_{k,u}^s = Y_0^s$ , then

$$K_{write} = E / Y_0^s \tag{3}$$

**B. CORRECTNESS**

Now gives the correctness verification.

$$(1) EE_k / Y_{k,u}^s = EE_k / e(g, g)^{p(0)s} = Y_{k,u}^s \square K_{rk} / \prod e(g, g)^{p(i)s \Delta_{i,s}(0)} = K_{rk}$$

$$K_{read} = K_{r1} \parallel \dots \parallel K_{r|LEB|}, M = D_{K_{read}}(C_r).$$

$$(2) e(g, \sigma) = e(g, h^s) = e(g^s, h) = e(P_u, h)$$

$$(3) E / Y_0^s = E / (Y_{CA}^s \prod_{k=1}^K Y_{k,u}^s)$$

$$= E / (e(E_{CA}, D_{CA}) \prod_{k=1}^K e(g, g)^{p(i)s \Delta_{i,s}(0)})$$

$$= K_{write}$$

**C. SECURITY**

In vMA-ABE-DP, not only the confidentiality of data is guaranteed, but the integrity of data and authenticity of data sources are verified. So the security of the scheme includes two parts: data confidentiality and signature unforgeability. Data confidentiality will be proved under selective-ID model, and signature unforgeability will be proved under adaptive selective-message attack.

**Theorem 1.** This scheme is sid-secure according to definition 4.

First we give some explain about behind proof. Then we follow with a detail proof.

*About confidentiality:* In our scheme, there are two kinds of permissions, which have been obtained by two different decryption respectively, the attribute authority number of the user must go to is different, too. Especially, the central authority need not take part in the first kind of decryption. The two processes involve the confidentiality, but the details are different, we will give proofs distinctly.

*About Read Permission:* Getting this kind of permission only need some authority, at least one. The adversary is allowed to request secret key for a given user  $u$  and attribute set  $A_u$  as long as there remains one honest authority  $k$  such that  $|A_C^k \cap A_u^k| < d_k$ . Thus, in the worst case, for all but one authority  $k$ , the adversary will be able to compute  $Y_{k,u}^s = e(g, g)^{y_{k,u}^s}$  for additive share  $y_{k,u}$ . We need  $K_{rk} = EE_k / Y_{k,u}^s$  to be something which the adversary cannot compute ( $e(g, g)^{\frac{ab}{c}}$  is indistinguishable from random). Thus, we must "embed" this incomputable value in the share  $y_{k,u}$  for the authority from which the adversary does not have sufficient attributes. Since, in the process of decryption  $K_{rk}$ , only need to meet the requirements of one authority, so the prove process may look on as a single authority scheme.

*About Write Permission:* The process of encryption and decryption is same as Chase's, so the detailed proof see literature [12].

*Proof:* The confidentiality proof of the scheme comprises two stages, one is to get  $K_{read}$  to decrypt the encrypted message, the other is to get  $K_{write}$ .

*The first stage:* Suppose there exists a polynomial-time adversary,  $A$ , that can attack our scheme in the Selective-ID model with advantage  $\epsilon$ . The challenger  $C$  that can play the Decisional MBDH game with advantage  $\frac{\epsilon}{2}$ . The simulation proceeds as follows:

The challenger sets the groups  $G_1$  and  $G_2$  with an efficient bilinear map,  $e$  and generator  $g$ . The challenger flips a fair binary coin,  $\mu$ , outside of  $C$ 's view. If  $\mu = 0$ , the challenger sets  $(A, B, C, Z) = (g^a, g^b, g^c, e(g, g)^{\frac{ab}{c}})$ ; otherwise it sets  $(A, B, C, Z) = (g^a, g^b, g^c, e(g, g)^R)$  for random  $a, b, c, R$ .

**Setup** The adversary sends an attribute set  $A_C^k$  for an honest authority. The challenge generate the public key parameters as follows. Given  $Y_k = e(g, A) = e(g, g)^a$ , chosen random  $\beta_{k,i} \in \mathbb{Z}_p$ ,  $\{T_{k,i} = g^{c\beta_{k,i}}\}_{i \in A_C^k}$ , and  $\omega_{k,i} \in \mathbb{Z}_p$ ,  $\{T_{k,i} = g^{\omega_{k,i}}\}_{i \in A_u^k - A_C^k}$ .

**Secret Key Queries** The adversary  $A$  requests for private keys where the attribute set  $A_u^k$  satisfied  $|A_C^k \cap A_u^k| < d_k$ . We first define three sets  $\Gamma, \Gamma', S$  in the following manner:

$$\begin{aligned} \Gamma &= A_C^k \cap A_u^k \\ \Gamma &\subseteq \Gamma' \subseteq A_u^k \text{ and } |\Gamma'| = d - 1 \\ S &= \Gamma' \cup \{0\} \end{aligned}$$

Now, we define the decryption key components  $D_{k,i}$  for  $i \in \Gamma'$  as:

If  $i \in \Gamma : D_{k,i} = g^{s_i}$ , where  $s_i \in_R \mathbf{Z}_p$

If  $i \in \Gamma' - \Gamma : D_{k,i} = g^{\frac{\lambda_i}{\alpha_{k,i}}}$ , where  $\lambda_i \in_R \mathbf{Z}_p$

The intuition behind these assignments is that we are implicitly choosing a random  $d - 1$  degree polynomial  $p(x)$  by choosing its value for the  $d - 1$  points randomly in addition to having  $p(0) = a$ . For  $i \in \Gamma$  we have  $p(i) = c\beta_{k,i}s_i$  and for  $i \in \Gamma' - \Gamma$  we let  $p(i) = \lambda_i$ .

The challenger  $C$  can calculate the other  $D_{k,i}$  values where  $i \notin \Gamma'$  since the challenger knows the discrete log of  $T_{k,i}$  for all  $i \in A_u^k - A_C^k$ . The challenger makes the assignments as follows:

If  $i \notin \Gamma'$ :

$$D_{k,i} = \left( \prod_{j \in \Gamma} C^{\frac{\beta_{k,j} \Delta_{j,S(i)}}{\alpha_{k,j}}} \right) \left( \prod_{j \in \Gamma' - \Gamma} g^{\frac{\lambda_j \Delta_{j,S(i)}}{\alpha_{k,j}}} \right) Y^{\frac{\Delta_{0,S(i)}}{\alpha_i}}$$

Using interpolation  $C$  is able to calculate  $D_{k,i} = g^{\frac{p(i)}{i}}$  for  $i \notin \Gamma'$  where  $p(x)$  was implicitly defined by the random assignment of the other  $d_k - 1$  variables  $D_{k,i} \in \Gamma'$  and  $Y_{k,u}$ . Therefore, the simulator is able to construct a private key for the attribute set  $A_u^k$ .

**Challenge** The adversary  $A$  submits two challenge messages  $M_0$  and  $M_1$  to the challenger. The challenger flips a fair binary coin,  $b$ , and returns an encryption of  $M_b$ . The ciphertext is output as:

$$C_{rb} = E_{K_{read}}, \{E_{k,i} = B^{\beta_i}\}_{i \in A_C}, EE_k = e(g, A)^{\frac{s_i}{c\beta_{k,i}}} \cdot K_{rk}$$

If  $\mu = 0$ , then  $Z = e(g, g)^{\frac{ab}{c}}$ . If we let  $r' = \frac{b}{c}$ , then we have  $E_0 = e(g, g)^{\frac{ab}{c}} \cdot K_{rk} = e(g, g)^{ar'} \cdot K_{rk} = Y_k^{ar'} \cdot K_{rk}$  and  $E_{k,i} = B^{\beta_{k,i}} = g^{b\beta_{k,i}} = g^{\frac{bc\beta_{k,i}}{c}} = g^{r'c\beta_{k,i}} = (T_{k,i})^{r'}$ . Therefore, the ciphertext is a random encryption of the message  $M_b$  under  $A_C$ .

Otherwise, if  $\mu = 1$ , then  $Z = e(g, g)^R$ . We then have  $E_1 = e(g, g)^R \cdot K_{rk}$ , since  $R$  is random,  $E'$  will be a random element of  $G_2$  from the adversary's view and the message contains no information about  $M_b$ .

**More Secret Key Queries** The challenger acts exactly as it did above.

**Guess**  $A$  will submit a guess  $b'$  of  $b$ . If  $b = b'$  the challenger will output  $\mu' = 0$  to indicate that it was given a MBDH-tuple, otherwise it will output  $\mu' = 1$  to indicate it was given a random 4-tuple.

In the case where  $\mu = 1$  the adversary gains no information about  $b$ . Therefore, we have  $\Pr[\mu' \neq \mu | \mu = 1] = \frac{1}{2}$ . Since the challenger guesses  $\mu' = 1$  when  $b \neq b'$ , we have  $\Pr[\mu' = \mu | \mu = 1] = \frac{1}{2}$ . If  $\mu = 0$  then the adversary sees an encryption of  $M_b$ . The adversary's advantage in this situation is  $\epsilon$  by definition. Therefore, we have  $\Pr[b = b' | \mu = 0] = \frac{1}{2} + \epsilon$ . Since the challenger guesses  $\mu' = 0$  when  $b = b'$ , we have  $\Pr[\mu = \mu' | \mu = 0] = \frac{1}{2} + \epsilon$ . The overall advantage of the challenger in the decisional MBDH game is



$\frac{1}{2} \Pr[\mu' = \mu \mid \mu = 0] + \frac{1}{2} \Pr[\mu' = \mu \mid \mu = 1] - \frac{1}{2} = \frac{1}{2}(\frac{1}{2} + \epsilon) + \frac{1}{2} \cdot \frac{1}{2} - \frac{1}{2} = \frac{1}{2} \epsilon$  The second stage): The same as in [12].

**Theorem 2.** The signature scheme in vMA-ABE-DP is secure against existential forgery on adaptive chosen-message attacks in Random Oracle Model if BLS signature is secure against existential forgery on adaptive chosen-message attacks.

*Proof:* The signature of the scheme is BLS short signature. Since BLS signature is secure against existential forgery on adaptive chosen-message attacks, so ours is.

## DISCUSSION

### A. DISCUSSION

In the scheme, we encrypt secret keys  $K_{read}$  instead of message  $M$ , alleviating the burden of encryption.  $K_{read}$  is divided into  $LEB$  parts and encrypted, which avoiding an adversary obtains  $M$  with  $l < LEB$  parts and enhancing the security of the scheme.

We combine the symmetric and asymmetric key system effectively. The mixed encryption mechanism (To ensure efficient encryption using symmetric key encryption of data, the encryption key is encrypted with the public key cryptosystem), ensure illegal users not to get encryption key.

Prevent illegal users and malicious users destroying information of the legitimate and honest users in the system. One side, the signature can be used to verify the message sources; on the other side, even if illegal users can crack encrypted data, they can not write data to the legitimate user message for not knowing  $K_{write}$ , illegally modified data can also be checked out.

### B. COMPARISON

About the number problem of authorities, which the user must go to before he can decrypt a message, was discussed in our scheme and Chase's, but there was some limit in Chase's. Now we will give some comparison followed.

1) We remove this problem by increasing a public key  $Y_{k,u} = e(g, g)^{y_{k,u}}$  by each attribute authority. The encryptor include  $EE_k = Y_{k,u}^s \cdot K_{rk}$  in the encryption based on  $LEB = \{k \mid A_C \cap A_u \geq d_k\}$ . To decrypt a message without to go to authorities that not in  $LEB$ . In Chase's scheme, he added one "authority attribute  $k$ " for each authority and a corresponding  $T_{Nk} = g^{t_{Nk}}$  to the public key, the central authority gave every user a secret key for each authority:  $D_{Nk} = g^{y_{k,u}/t_{Nk}}$ . The encryptor would include  $T_{Nk}^s$  in the encryption for these authorities without required any attributes and a user would combine  $T_{Nk}^s$  and  $D_{Nk}$  while decryption. We can make a conclusion that the central authority and the encryptor are involved as generating access policy in Chase's while only encryptor did in ours, which reduce the dependence on the central authority's, more easily extended to semi-trusted authority or no trusted authority scheme.

2) Chase et al. made an extension to let the user to go to at least  $D$  authorities while decryption, yet in our scheme, it can bear arbitrary number authority specified by encryptor. As a result, ours is more flexible in application.

3) In the above process, there is added some information in both schemes. We assume that there is only a user,  $K$  attribute authorities,  $x$  attribute authorities without required any attribute in [12],  $|LEB|$  attribute authorities involved while decryption in our scheme. The comparison of added information is shown in Table II. In [12], increased one authority attribute  $k$  and one public key for each attribute authority, increased every user a secret key  $D_{Nk}$  for each attribute authority, increased  $T_{Nk}^s$  in the encryption for  $x$  authorities without required any attributes, the total increased communication is  $K|k| + 2K|p| + x|p|$ . Yet, in our scheme, increased a public key for each attribute authority and  $|LEB| EE_k$ , the total increased communication is  $(K + |LEB|)|p|$ . While decryption, there still needs to compute  $K e(g, g)^{y_{k,u}^s}$  in [12], the amount of computation does not increase nor decrease.

However, it only needs to compute  $|LEB| e(g, g)^{y_k u^s}$  in our scheme, where  $1 \leq |LEB| \leq K$ , so the amount of computation reduced at least  $K - |LEB|$ . Thus, from the analysis of increased communication and computation, our scheme is significantly better.

Table.2 Additional Information

Item	[12]scheme	Our scheme
Each attribute authority	a authority attribute $k$ a public key $T_{Nk}$	a public key
Central authority	$K$ secret key $D_{Nk}$	0
ciphertext	$x T_{Nk}^s$	$ LEB  EE_k$
decryption	0 computational cost	$-(K -  LEB )$ computational cost

## CONCLUSION

We create a novel scheme of verifiable multi-authority attributebased encryption. Our scheme allows users having different attributes to obtain different access permissions. In the process, the number of authority is not fixed. All these are done by encrypt easily. Our system allows decrypt to verify the integrity of data and realness of encryptor who provided a signature on message.

Next, it would be interesting to consider much more access permission in attributes based encryption scheme. With the rapid development of cloud compute, we will apply it in cloud storage.

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