Research on the new load patterns for multi-roller stretch forming process

Zhang Wei-chuan[a]*, Li Yong-feng[a] and Li Ming-zhe[b]

[a]*Key Laboratory of Automobile Materials of Ministry of Education, College of Materials Science and Engineering, Jilin University, Renmin Street, Changchun, China*
[b]*Dieless Forming Technology Center, Jilin University, Renmin Street, Changchun, China*

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ABSTRACT

Multi-roller stretch forming process (MRSF) is a flexible manufacturing technique to form sheet panels into different curvature. Based on the geometrical relationship of 3D surface stretch forming by MRSF, an inscribed arc of the roller's critical position has been established by adopting geometric analytical method. With the arc, the variation regulation of loading force on each roller is obtained using the principle that the stretch force on each roller stays the same in all places. Numerical simulations have been done for forming the 08Al spherical parts by MRSF with the equal force and variable force loading methods respectively. The results show that the flexibility, die fittingness, strain and stress distribution as well as the quality of variable force loading by MRSF are the best among these types, equal force loading method is a little worse than the former, however the traditional stretch forming process with rigid-clamps (RCSF) is not flexible and it is hard to make the blank and die jointed. In addition, the phenomenon of stress concentration is serious and the quality of the formed parts is the worst.

Key words: Flexible stretch forming, Loading pattern, Spherical part, Numerical simulation
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INTRODUCTION

Traditional stretch forming process mainly depends on the movement of grippers and the lifting of the stretching machine table so as to make the blank jointed with the die surface to form the final part shape [1].

The blank appears strain concentration phenomenon made by the traditional stretch forming machine with integral clamps, especially when there is bidirectional large curvature, which may influence the quality of the formed part much [2, 3].

What is more, the load control method of traditional stretch forming is very complex, which needs repeatedly trial-stretching to confirm the optimal load track and relies on practical experience extremely, which can lead to unstable forming quality[4-6].

A Multi-roller flexible stretch forming experimental device has been developed by Jilin University. The device adopts force-loading pattern and has many advantages, such as simple structure, low cost, easy-controlled, etc. [7].

Fig.1 is the flexible roller stretch forming device, composed of flexible structure of roller device and flexible structure of clamp device which is made up of a number of clamps swinging around some certain axes [8].

Firstly, the blank is fixed by flexible clamps device. Secondly, the discrete rollers move downward vertically to the blank, until the blank joints with the die.

During the forming process, each roller is given properly down force to make sure that the blank is stretched equally and has uniform strain distribution on the each position where the rollers stop [9,10] .

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In this paper, the inscribed arc of the roller's critical position when the blank joints with the die completely are established by adopting geometric analytical method. Combining with Newton's dynamical theory with the arc, each roller's optimal load model is calculated.

Through numerical simulation and experimental test, it shows that the quality of spherical shaped parts with variable load force is better than that with invariable force using flexible roller stretch forming which is also better than the traditional stretch forming with rigid clamps. In addition, the results prove the feasibility of variable load force and provide some reference to the development of multi-roller stretch forming device and the processoptimization [11-13].
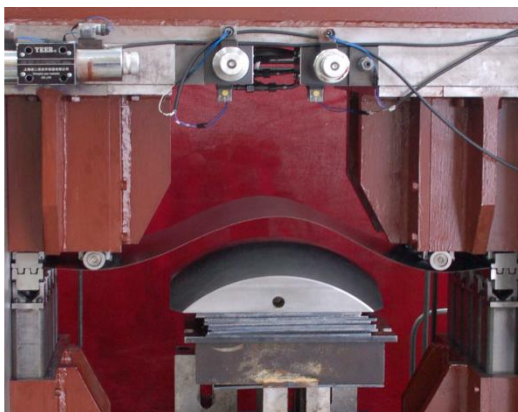

Fig.1 Multi-roller stretch-forming device

2. GEOMETRIC MODEL OF MULTI-ROLLER STRETCH FORMING

In order to analyze the inscribed arc of the roller's critical position theoretically, some corresponding assumptions can be made. In this paper, the thickness of blank can be neglected during calculating the parameters because the blank is very thin.Fig.2 is the schematic diagram of multi-roller flexible stretch forming principle(1/2 model).

Fig.3 is the geometric schematic diagram of a plane cut by the plane γ(x=0) .The device adopts floating clamps and the friction and inertial force of cylinder are neglected, so EQ can be regarded as a horizontal line.

When the rollers move downward to a certain position, the blank can joint with the die completely with the effect of the rollers. The ordinate of the tangency point E between the roller and blank is z_E, accordingly, the descending distance of rollers is $H=z_0-z_E$. z_0 is the distance from the vertices to bottom of the die.
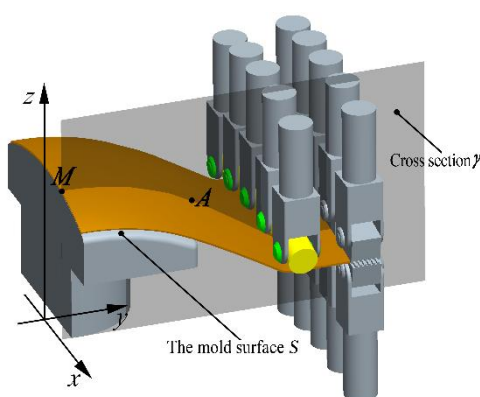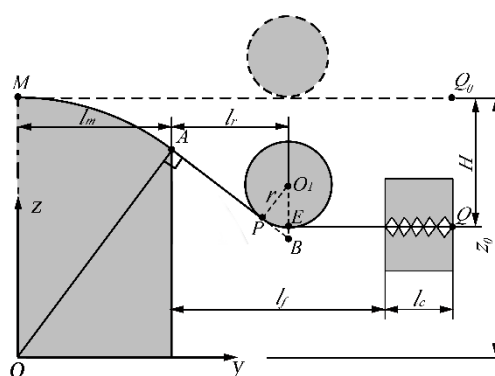

Fig.2 The principle schematic diagram   Fig.3 The geometric schematic diagram of Multi-roller flexible
stretch   forming of Multi-roller flexible stretch forming

2.1. CRITICAL FITTINGNESS CONDITION OF SHEETMATERIAL

Without loss of generality, the forming surface of any die can be described as S and its equation is $F(x,y,z)=0$.The surface S is cut by plane γ(x=x_i) which is vertical to x-axis, correspondingly, AM is the section line, which can be described as $z = \varphi(x_i, y)$, the ordinate of A is $z_A = \varphi(x_i, l_m)$.

The slope the *A* point is $k_A = \dfrac{dz}{dy} = \dfrac{d\varphi(x_i, y)}{dy}$, the slope of line AB tangent to curve AM is

$$k_{AB} = k_A = \frac{d\varphi(x_i, y)}{dy}\bigg|_{y=l_m} = K(x_i, l_m)$$, that is

$$k_{AB} = \frac{\varphi(x_i, l_m) - z_B}{-l_r} = K(x_i, l_m)$$, so

$$z_B = \varphi(x_i, l_m) + l_r K(x_i, l_m) \tag{1}$$

According to the geometric relations,

$$\overline{BE} = r\left(\sqrt{1 + K^2(x_i, l_m)} - 1\right) \tag{2}$$

$$z_E = z_B + \overline{BE} \tag{3}$$

Put the equation (1) and (2) into equation (3),

$$z_E = \varphi(x_i, l_m) + l_r K(x_i, l_m) + r\left(\sqrt{1 + K^2(x_i, l_m)} - 1\right) \tag{4}$$

For spherical-shaped die with radius R_0, the surface equation of die is

$$x^2 + y^2 + z^2 = R_0^2$$

For any given section plane curve $\gamma(x=x_i)$, it fits to the equation $z^2 = R_0^2 - (x_i^2 + y^2)$, taking partial derivative of the equation with respect to y , the slope of line *AB* can be described as

$$k_{AB} = \frac{dz}{dy}\bigg|_{y=l_m} = K(x_i, l_m) = -\frac{l_m}{\sqrt{R_0^2 - (x^2 + l_m^2)}} \tag{5}$$

Put equation (5) into (4):

$$z_E(x) = \sqrt{R_0^2 - (x^2 + l_m^2)} - \frac{l_m l_r}{\sqrt{R_0^2 - (x^2 + l_m^2)}}$$
$$+ r\left(\sqrt{1 + \frac{l_m^2}{R_0^2 - (x^2 + l_m^2)}} - 1\right) \tag{6}$$

From equation (6), we can know that in order to make the blank jointed with the die completely, tangent point E has to satisfy the inequality $z(x_i) \leq z_E(x_i)$.

2.2 RELATIONSHIP BETWEEN STRETCHFORCE T AND LOADING FORCEF
In order to obtain the relationship between stretch force and loading force, the geometric relationship is simplified like Fig.4a which shows that the normal pressure N_E and loading force *F* satisfy the equation approximately at the position of point *E*:
$N_E = F\cos\beta$(7)

It can be seen from Fig.4b that the maximum stretching force T_{max} given by the rollers to the blank and normal pressure N_E satisfy the relationship:

$$N_E = 2T_{max} \sin\frac{\theta}{2}\cos\frac{\theta}{2} = T_{max}\sin\theta \tag{8}$$

Combining equations (7) with (8), the following expression is obtained.

$$F = \frac{\sin\theta}{\cos\beta}T_{max} \tag{9}$$

As the Fig.4c shows, T_{max} can be divided into *ox* and *oy* directions of the component, they are the lengthwise direction stretch force T_{oy} and width direction stretch force T_{ox}.

Here $T_{\max}=T_{oy}/cos\alpha$ (10)

Put equation (10) into (9):

$$F = \frac{\sin\theta}{\cos\beta}T_{\max} = \frac{\sin\theta}{\cos\alpha\cos\beta}T_{oy} = kT_{oy}$$ (11)

Where T_{oy} is the maximum width direction stretch force, so T_{oy} is a constant when the blank is given certain material, thickness and elongation. So k is the coefficient of variation gradient of loading force F.

It can be got from the geometrical relationship shown in Fig.4c that:

$$\left.\begin{array}{l} \cos\alpha = \dfrac{l_m+l_r}{\sqrt{\left(l_m+l_r\right)^2+x^2}} \\[2ex] \cos\beta = \dfrac{1}{\sqrt{\tan^2\beta+1}} \\[2ex] \sin\theta = \dfrac{l_m}{R_0} \end{array}\right\}$$ (12)

Combining equation (11) and (12),the following expression is obtained.

$$k = \frac{l_m\sqrt{\tan^2\beta+1}}{R_0(l_m+l_r)}\sqrt{\left(l_m+l_r\right)^2+x^2}$$ (13)

The slope of any point on the curve can be described as $K(x) =dz_E(x)/dx=-\tan\beta$ by making derivative to x of $z_E(x)$ in equation (6), so the $\tan\beta$ in equation (13) is given by the expression

$$\tan\beta = -\frac{dZ_E(x)}{dx} = \frac{\left(R_0^2-l_m^2+l_m l_r\right)x-x^3-\dfrac{l_m^2 r x}{\sqrt{R_0^2-x^2}}}{\left(R_0^2-x^2-l_m^2\right)^{3/2}}$$ (14)
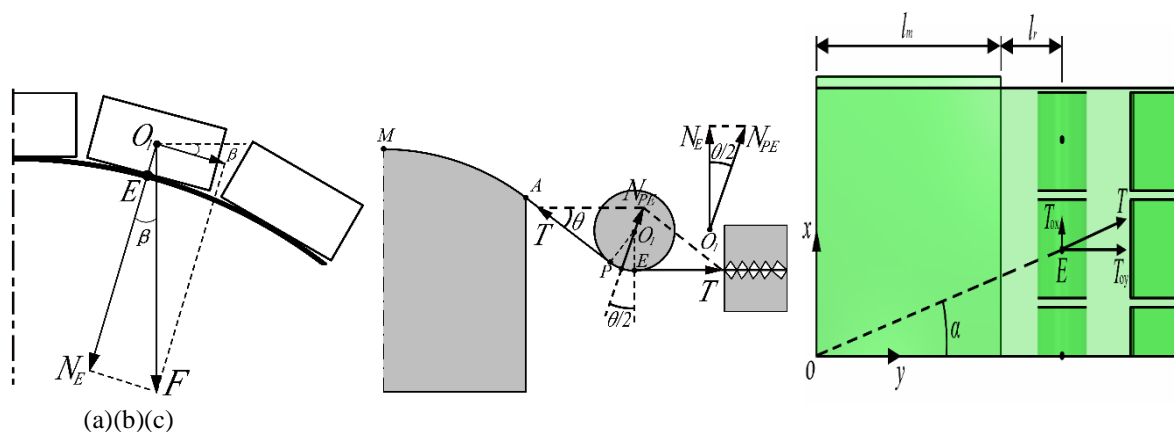

(a)(b)(c)

Fig.4 Relationship between stretch force and loading force

3NUMERICAL CALCULATION
The software ABAQUS is chosen to simulate the multi-roller stretch forming process. The material of sheetmaterial is 08AL and its basic size is $600\times240\times1$mm.The radius R_0 of spherical-shaped die is 300mm, the dimensions ofdie are 300×250mm.The process parameters in the simulation are lm=150mm,l_r=50mm,r=20mm,l_f=110mm,l_c=40mm.

Regarding symmetry center O of the blank as coordinate origin, the coordinates of each roller center in the line of x-axis are respectively: x_1=0, x_2=48, x_3=96.

3.1. CRITICAL LINE OF DIEFITTINGNESS
Put the above parameters into equation (6),the roller's ordinate $z_E(x_i)$ can be calculated and downward displacement

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amount of roller is $H_i=z_0-z_E(x_i)$,for spherical-shaped part, $z_0=R_0$.

Table 1 is the maximum ordinate, minimum downward displacement amount of each roller and the force given by roller to the blank at the critical position.

A critical line (as shown in Fig.5) is obtained to evaluate whether the blank joints with the die completely according to numerical simulation.Fig.5 illustrates that when the ordinate z_E of point E is below under the critical line, it means the blank joints well, otherwise not.

Table 1 The parameters of rollers when attaching die

Roller	Ordinate z_E	Amount H_i	Force on blank F
Roller 1	234mm	66mm	4.92kN
Roller 2	229mm	71mm	5.31kN
Roller 3	214mm	86mm	7.92kN

3.2 COEFFICIENT OF VARIATION GRADIENT

The changing relation curve between the coefficient k and the distance from roller center to point D is obtained from the formulas (10) and (11), at this time loading force F can ensure the lengthwise direction stretch force T_{oy} loaded by rollers are uniform as shown in Fig.6.The corresponding k are $k_1=0.50$, $k_2\approx0.5249$, $k_3\approx0.6055$ when $x_1=0,x_2=48,x_3=96$.

For the quarter model, the loading force of Roller1, Roller2 and Roller3 are $F_1/2, F2, F3$and they accord with the relationship: $F_1/2+F_2+F_3=F_{total}/4$,in which, F_{total} is the total loading force of all rollers. Utilizing the equations $F_1=k_1T_{oy},F_2=k_2T_{oy},F_3=k_3T_{oy}$,that is
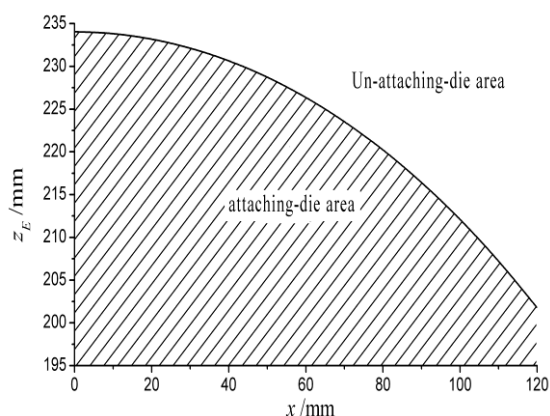
$$T_{oy}\approx0.1811F_{total} \quad (15)$$

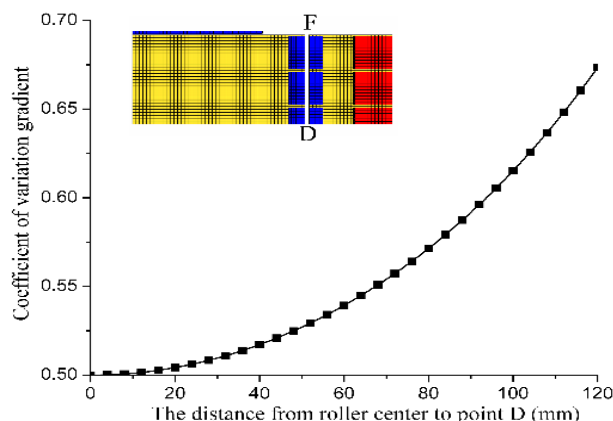Fig.5 The critical line of attaching-die　　　　Fig.6 The coefficient of variation gradient of different positions

4. SIMULATION ANALYSIS AND EXPERIMENT VALIDATION

According to simulation results, the maximum loading force of different stretch forming processes should be greater than or equal to the force on the blank by Roller3 when all rollers are in critical positions in order to ensure the blank joint with the die completely in different loading patterns. From Table 1, the force on the blank loaded by Roller3 is 7.92kN, rounding up the result, so $F_{max}=8.0$kN.

In order to compare the precision of different loading patterns formed parts, the force of traditional stretch forming rigid clamps should be equal to the total loading force of all rollers of multi-roller stretch forming.

Table 2 The loading force of rollers in different loading patterns

Loading pattern	Roller1/ kN	Roller2/ kN	Roller3/ kN	Total force/ kN
Equal force	4.00	8.00	8.00	20.00
Variable force	3.62	7.60	8.77	19.99

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Based on 1/4 model, Put F_{total}=80kN into equation (17), there are $T_{oy} \approx 14.49$kN. The value of $F_1/2$, F_2 and F_3 are 3.62kN, 7.60kN and 8.77kN by multiplying T_{oy} with corresponding variation coefficient k_1, k_2 and k_3, as shown in Table 2.

4.1. THE RESULT OF NUMERICAL SIMULATION

Fig.7 shows the relation curve between the ordinate z_E of tangent point E with the distance from tangent point E to point D for different loading patterns. From Fig.7, the attaching-die width of the blank reaches to 120mm by adopting multi-roller stretch forming with variable force loading, simultaneously, the blank joints to the die completely. However the attaching-die width are merely 108mm and 88mm respectively by using multi-roller stretch forming with equal farce loading and traditional stretch forming with rigid clamps.

Therefore the flexibility, die fittingness, strain and stress distribution as well as the quality of variable force loading by MRSF are the best among these types, equal force loading method is a little worse than the former, however the traditional stretch forming process with rigid-clamps (RCSF) is not flexible and it is hard to make the blank and die jointed well. In addition, the phenomenon of stress concentration is serious and the quality of the formed parts is the worst. That is because the concentration force is dispersed to the discrete rollers that can arrange in a curve related to the end surface of the die, which will improve the flexibility and avoid the stress concentration phenomenon. Under the circumstance of multi-roller stretch forming with variable force loading, the loading force of each roller changes regularly according to the shape of the die's end surface, making the stretch force to the blank by the roller more uniform and making die fittingness easier.
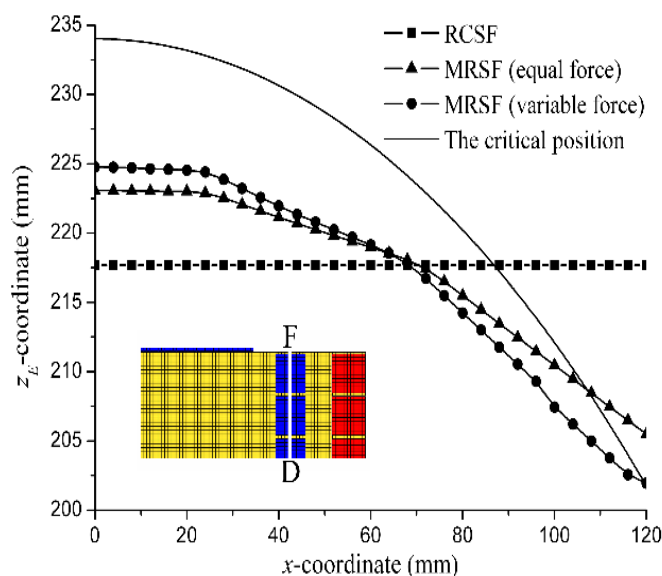

**Fig.7 Z$_E$ varies with x in different loading patterns**

Fig.8 is the strain distribution of spherical surface parts in *y* direction using different stretch forming process. Fig.8 (a), (b) and (c) present that the value difference between center and margin of the spherical part and strain distribution using multi-roller stretch forming with variable force loading is smaller than the one using multi-roller stretch forming with equal force loading, however, the one using traditional stretch forming with rigid clamps have obvious strain concentration and non-uniform plastic strain distribution.

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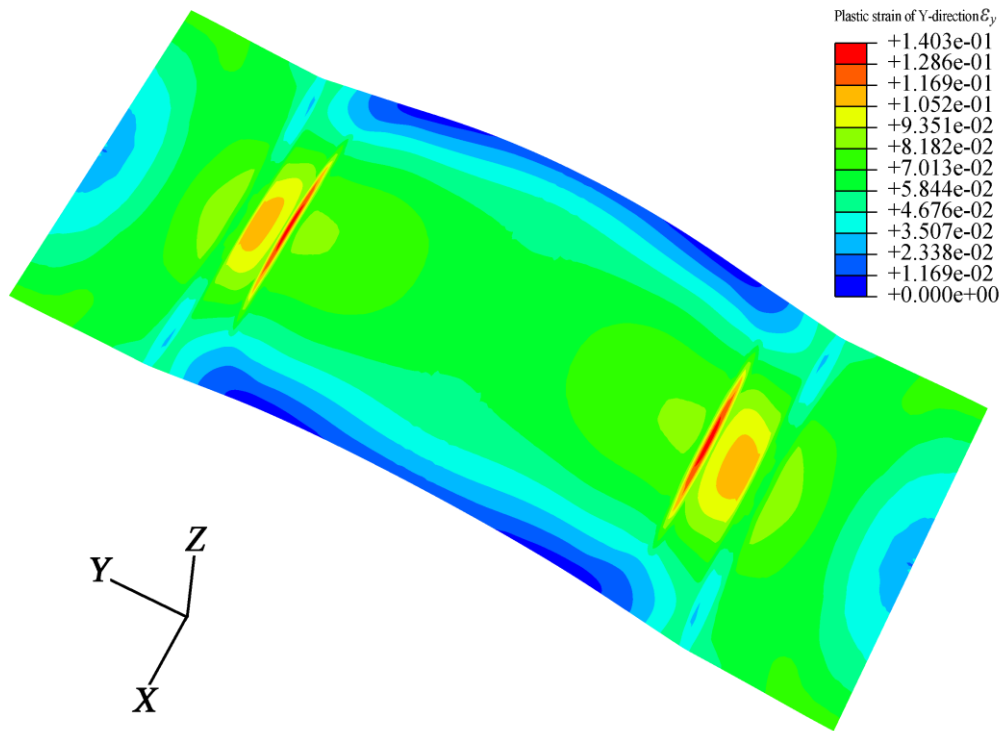
(a) The traditional stretch forming process with rigid clamps
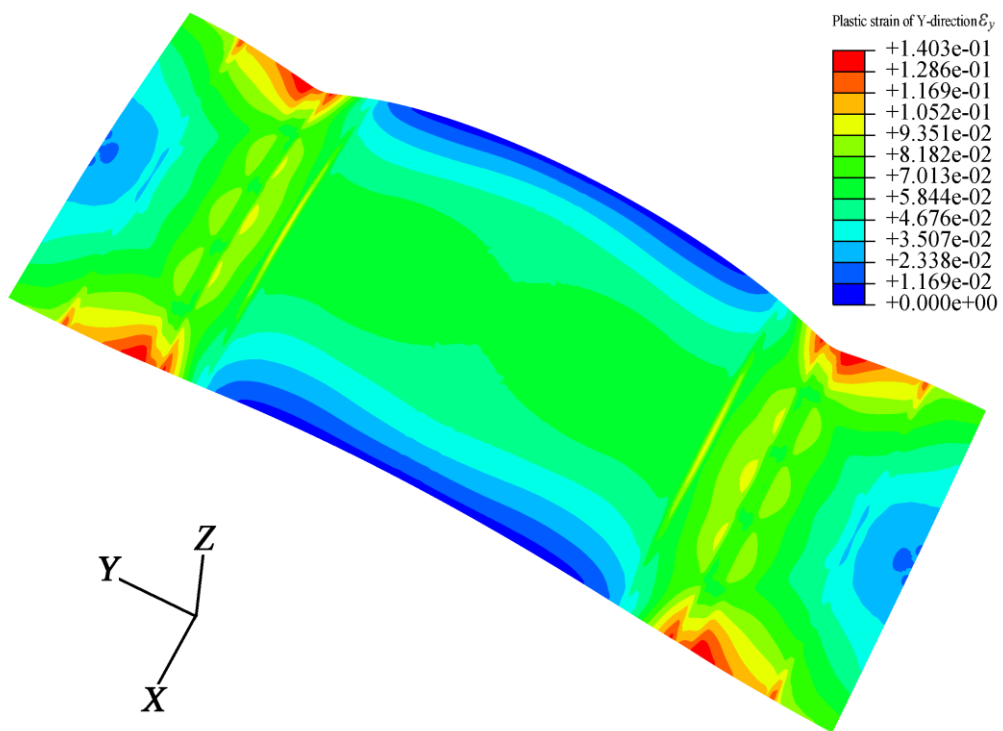
(b)Multi-roller stretch forming process (equal force loading)

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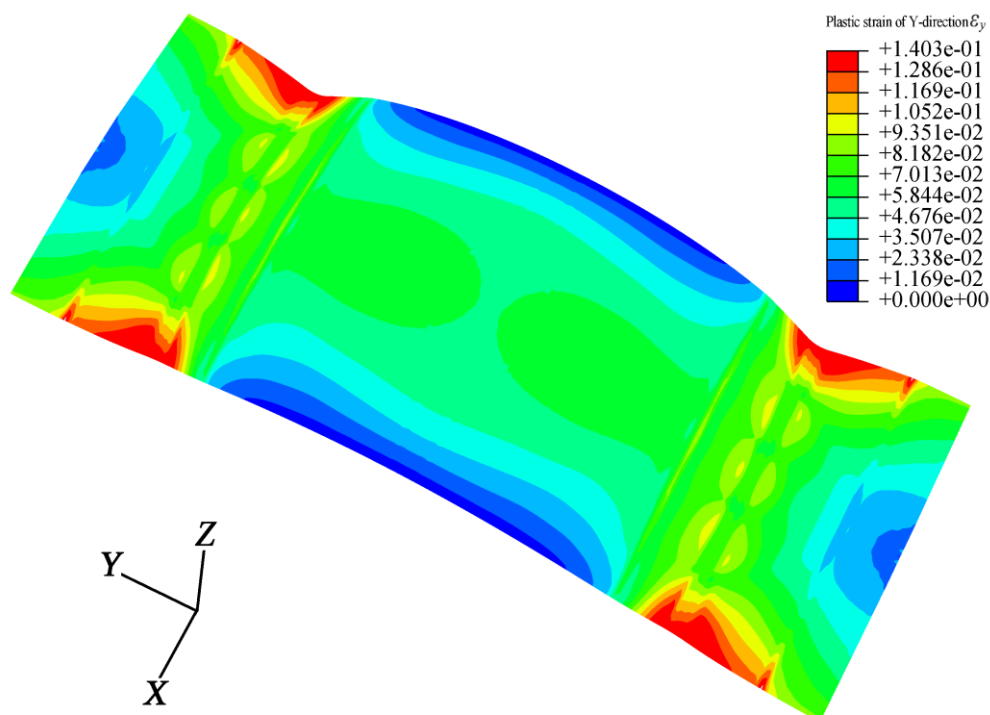
(c) Multi-roller stretch forming process (variable force loading)
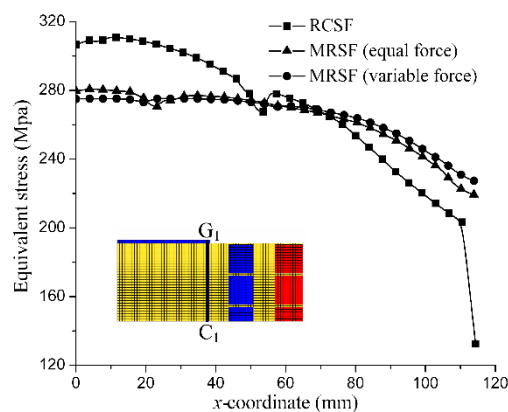**The plastic strain distribution in y direction**
Fig.8 The plastic strain distribution in y direction of different stretch forming process.

In the blank width direction of spherical part extract the equivalent stress values and equivalent plastic strain values respectively of each node (on line CG and C_1G_1)where the stress distribute most non-uniform of different stretch forming process and draw the curve as shown in Fig.9 and Fig.10.

The value difference between the maximum and the minimum equivalent stress of spherical part using multi-roller stretch forming with variable force loading is smaller than the one using multi-roller stretch forming with equal force loading and the one using traditional stretch forming with rigid clamps is the biggest and the stress distribution is most non-uniform, shown in Fig.9.Similarly, the Fig.10 shows the same regulation of equivalent plastic strain distribution.
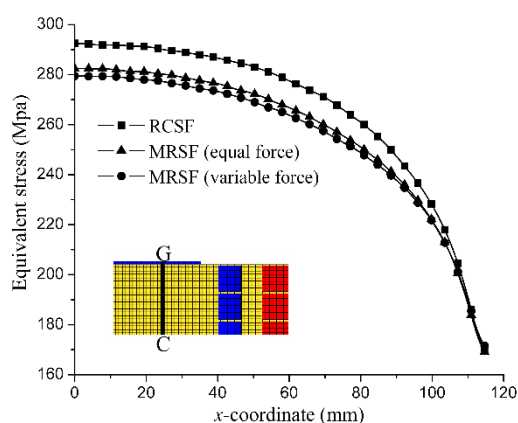
(a) The equivalent stress curve on line CG   **(b) The equivalent stress curve on line C_1G_1**

Fig.9 The equivalent stress curve in blank width direction (on line CG and C_1G_1)

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(a) The equivalent plastic strain curve on line CG   (b) The equivalent plastic strain curve on line C_1G_1
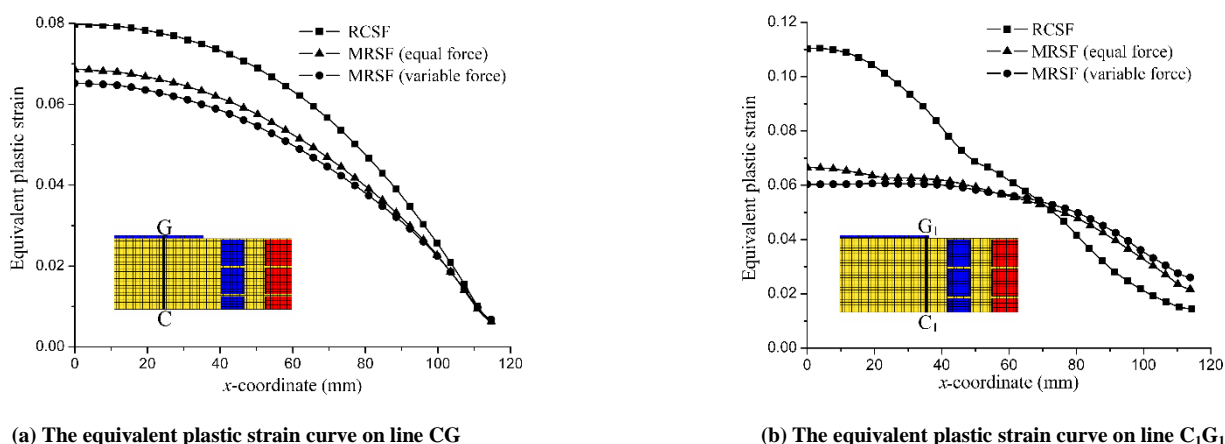
Fig.10 The equivalent plastic strain curve in the blank width direction (on line CG and C_1G_1)

4.2 EXPERIMENT VALIDATION

Based on above numerical simulation and analysis, a stretch forming experiment on 08AL sheet blank (the area is $600\times240mm^2$, the thickness is1mm) is designed, adopting the loading force shown in Table 2.Fig.11 shows the formed spherical-shaped part by multi-roller stretch forming device. The formed spherical-shaped part has a good curvature in width direction, as shown in the Fig.11. This process is suitable for forming bidirectional large curvature surface part and the surface of effective formed area is smoother.

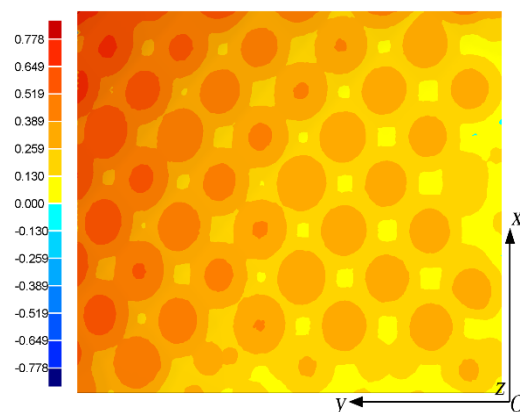**Fig.11 The spherical parts formed by MRSF prototype**   **Fig.12 Error comparison between experimental results and numerical simulation results**

Measure the spherical-shaped part after spring back by 3D scanner and extract the nodes data information of part surface. Comparing it with the nodes information of numerical simulation results, the error comparison diagram is drawn, as shown in Fig.12.The figure shows that the error between experimental results and numerical simulation results is small and almost distributes in -0.375 to 0.625.This means the numerical simulation results are almost in accord with the experimental ones.

CONCLUSION

MRSF is a new flexible stretch forming process. The loading force changing rule for the uniform stress of the blank is obtained through geometric analysis and Newton's dynamical theory. Extensive numerical simulations of MRSF processes have been performed by dynamic explicit finite element methods, a series of numerical results are obtained, these results reveal the effects of different loading patterns on the sheet metal deformation.

The main points are concluded as follows:
1) The critical line of die fittingness is obtained with the geometric relationship of flexible roller stretch forming, it can be used to evaluate and judge the maximum die fittingness width, providing some guidance for simulation and experiment.
2) The changing rule of loading force on rollers is obtained based on the principle that the stretch force on the blank by roller is the same in all positions. The loading force on each roller can be calculated by using this rule, providing

some guidance for the simulation of flexible roller stretch forming with variable force loading process and stretch parts.

3) Comparing traditional stretch forming process with flexible roller stretch forming process by means of numerical simulation on spherical-shaped part (R300mm), the results indicate that the flexibility, the die fittingness performance, the strain distribution and the stress distribution of flexible roller stretch forming process loaded by the variable force are the best, then, by the equal force. The traditional stretch forming process with rigid clamps is not flexible, and it is hard for the blank to joint with the die, in addition, it has serious stress-concentration phenomenon, the quality of the formed parts is relatively bad.

Acknowledgments

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