



Research Article

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## Forecasting CO<sub>2</sub> emissions of power system in China using Grey-Markov model

Jie Xu<sup>1,2</sup> and Yuansheng Huang<sup>1</sup>

<sup>1</sup>School of Economics and Management, North China Electric Power University, Beijing, China

<sup>2</sup>College of Management, Hebei University, Baoding, China

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### ABSTRACT

The greenhouse effect and its extension affecting is one of the key issues to governments and academics currently. Study shows, CO<sub>2</sub> produced from burning fossil fuels are liable 2/3 of the above-mentioned problems. CO<sub>2</sub> emissions in China are mainly concentrated in the power plants. In this paper, Gray - Markov method is used for long-term load forecasting, combined with the prediction of power generation coal consumption value. Meanwhile, the carbon emissions of power system in 2020-2050 are estimated through the prediction. The results show that: the power system 2020, 2030, 2040 and 2050 carbon emissions are: 7.7254 billion tons, 20.0616 billion tons, 51.0740 billion tons and 131.3582 billion tons. Basis on that, we analyze the trend of power system low-carbon development. Then provide some suggestions to reduce CO<sub>2</sub> emissions of power system from the level of the national policy, the level of power generation components, power grid optimize and dispatching in the future.

**Key words:** Grey-Markov model, load forecasting, power system, CO<sub>2</sub> emissions

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### INTRODUCTION

With the rapid development of the global economy, carbon dioxide produced by excessive burning of fossil fuels caused global warming and serious environmental problems. As a result, global warming had become the environmental problems that the entire human society has to face, and attracted great attention worldwide.

China has achieved rapid economic development, at the same time the carbon dioxide emissions increased. At present, China's carbon dioxide emissions ranked first in the world exceeding the United States. According to the data of China Energy Report (2008) Carbon Emissions Research, carbon dioxide emissions in China are mainly concentrated in the power plants, industry and transportation, these three sectors' emissions are about 63-73% of total emissions. Power industry was one of the main sectors of carbon dioxide emissions in the national economy, its emissions are 38.76% of total emissions [1]. Therefore, the power industry has significant reduction space. Understanding the carbon emissions of power sector, and projecting its future development trend have great significance in lowering carbon dioxide emissions of the power industry.

To predict carbon emissions of the power system, we need accurately forecast the electricity demand. In order to achieve emission reduction targets established by the Chinese government, Power industry should accurately predict the power load, Make reasonable adjustments of the power structure while satisfying the demand of national economic development. When we understand the carbon emissions of power system, we can find ways to reduce carbon emissions. In this paper, the power system carbon emissions were predicted by predicting the power load using Gray - Markov model, combined with supply coal consumption predictive value. Based on the work, we put forward some suggestions of low-carbon power system development.

**RESEARCH METHODOLOGY**

For load forecasting, there is systematic research, current trend in power load forecasting technology is: extrapolation forecasting techniques, regression model forecasting techniques, time series forecasting techniques, gray prediction technology. Among them, the gray prediction technology is widely used in the short, medium and long term power load forecasting for small sample size, the higher the prediction accuracy [2]. On this basis, there is a lot of research of the application of improved gray prediction technology in load forecasting. This paper uses Grey - Markov model for load forecasting since Grey model needs small sample size but can give long term prediction. This paper uses gray rolling forecasting techniques, It uses GM (1,1) model to predict the next value, and then added them to the data at the same time removed the oldest value, keeping the number of columns constant. Then feed the data to the GM (1,1) model, repeating the process until the predetermined goal and prediction accuracy are reached. In the end, we combine with Markov techniques. Gray model and Markov chain can both be used for time series prediction, gray system changes the processing method for stochastic problems, it takes the randomness of the system as a gray, has application in systems when information is unknown or unclear. But Grey forecasting is generally used with less data, short time frame and little fluctuation, the predicted trend is a relatively smooth curve, monotonically decreasing or increasing. In the presence of random fluctuation, there will be predictions that are too high or too low. The Markov chain is the study of random variation system, an n-order Markov chain consists of a collection of n states  $\{a_1, a_2, \dots, a_n\}$  with a set of transition probability  $P_{ij}(i, j = 1, 2, \dots, n)$  to determine. In this process, any time can only be in one status, if in the state  $a_i$  at time k, then at time k + 1 in the state  $a_j$ , transition probability  $P_{ij}$  reflect the influence degree of each factor, so the Markov chain is suitable for predicting dynamic process with large random fluctuations, and makes up for the weakness of the gray prediction. The two models complement each other and provide a practicality.

The establishment of gray model GM (1,1)

GM (1,1) model established the differential equation after generating process to the raw data. Establish GM (1,1) model requires only a few columns  $X^{(0)}$ : Let

$$X^{(0)} = (X^{(0)}(1), X^{(0)}(2) \dots X^{(0)}(n))$$

Take the series 1-AGO (Accumulated Generating Operation), so

$$X^{(1)} = (X^{(1)}(1), X^{(1)}(2) \dots X^{(1)}(n)) =$$

$$X^{(1)}(1), X^{(1)}(1) + X^{(0)}(2) \dots, X^{(1)}(n-1) + X^{(0)}(n))$$

In the formula  $X^{(1)}(k) = \sum_{m=1}^k (X^{(0)}(m)) \quad k = 1, 2, \dots, n$

Generating the original series by the accumulation weakened the impact of bad data in original data, established the model after it became a regular sequence.

Using  $X^{(1)}$  to constitute albino differential equations:  $\frac{dX^{(1)}}{dt} + aX^{(1)} = u$

Solving Parameters  $a, u$  using the least square method

$$X = [a, u]^T = (B^T B)^{-1} B^T Y_N$$

$$B = \begin{pmatrix} -\frac{1}{2} X^{(1)}(1) + X^{(1)}(2) & 1 \\ -\frac{1}{2} X^{(1)}(2) + X^{(1)}(3) & 1 \\ \dots & \dots \\ -\frac{1}{2} X^{(1)}(n-1) + X^{(1)}(n) & 1 \end{pmatrix}$$

$$Y_N = [X^{(0)}(2), X^{(0)}(3), \dots, X^{(0)}(n)]^T$$

Get Gray model is:

$$\hat{X}^{(1)}(k+1) = [X^{(0)}(1) - \frac{u}{a}]e^{-ak} + \frac{u}{a}, (k = (0, 1, 2, \dots))$$

$$\hat{X}^{(0)}(k+1) = \hat{X}^{(1)}(k+1) - \hat{X}^{(1)}(k)$$

$$= (1 - e^{-a})[X^{(0)}(1) - \frac{u}{a}]e^{-ak}, (k = (0, 1, 2, \dots))$$

The establishment of improved Gray-Markov model

The basic idea of Grey-Markov prediction model is: first establish the gray GM model, obtained the fitted curve; according to fitting curve can be divided into several dynamic range, and then through the Markov transition probability matrix predict the next state, calculate the predicted values. Specific steps are as follows:

The first step: In accordance with the aforementioned improved gray model GM (1.1), calculated predicted value  $\hat{x}^{(0)}$ .

The second step: state divided

Let the original sequence is:  $x^{(0)} = \{x^{(0)}(1), x^{(0)}(2) \dots x^{(0)}(n)\}$

The analog values of original sequence is:  $\hat{x}^{(0)} = \{\hat{x}(1), \hat{x}(2) \dots \hat{x}(n)\}$

When the random sequence  $x^{(0)}$  meet the characteristics of Markov chain, divided  $(m+1)$  parallel curve to the variation curve  $\hat{x}(k)$  into  $m$  states  $F_1, F_2, \dots, F_m$ , where the value of  $m$  based on the original sequence and research object.

Firstly, forecasts for each thermal generating capacity using gray prediction model, obtains prediction residuals with actual and predicted value. Divides residual state as follows according to the proportion of the actual value, in this paper makes the load forecasting results as follows:

- (1) The residual proportion is down to -4%, which means that the value of power load forecasting has been seriously underestimated, called a state  $F_1$ ;
- (2) The residual proportion is in  $(-4\%, 0]$ , which means that the value of power load forecasting was normal underestimated, called a state  $F_2$ ;
- (3) The residual proportion is in  $(0, 4\%]$ , which means that the value of power load forecasting is normal overestimated, called a state  $F_3$ ;
- (4) The residual proportion is up to 4%, which means that the value of load forecasting was seriously overestimated, called a state  $F_4$ .

The third step: determined the state transition probability matrix

If  $M_i$  is the initial sequence of samples in the state  $F_i$ ,  $M_{ij}(m)$  is the initial data sample that  $F_i$  through the

$m$ -step transition to  $F_j$ ,  $p_{ij}(m) = \frac{M_{ij}(m)}{M_i}$  ( $i = 1, 2, \dots, n$ ) is called the state transition probability.

So the state transition probability matrix is:

$$P^{(m)} = \begin{bmatrix} P_{11}^{(m)} & P_{12}^{(m)} & \dots & P_{1n}^{(m)} \\ P_{21}^{(m)} & P_{22}^{(m)} & \dots & P_{2n}^{(m)} \\ \dots & \dots & \dots & \dots \\ P_{n1}^{(m)} & P_{n2}^{(m)} & \dots & P_{nm}^{(m)} \end{bmatrix}$$

The fourth step: forecasting

According to Markov prediction model  $s_1 = s_0 * P; s_2 = s_0 * P^2; \dots; s_n = s_0 * P^n$  can be predicted.

## DATA SOURCES

**Table 1: 2000-2010 China's power structure and composition**

Year	Gross power generation (billion kwh)	Thermal power		Hydropower		Nuclear power		Others	
		Production (billion kwh)	Proportion (%)	Production (billion kwh)	Proportion (%)	Production (billion kwh)	Proportion (%)	Production (billion kwh)	Proportion (%)
2000	1368.48	1107.92	80.96	243.13	17.77	16.74	1.22	0.69	0.05
2001	1483.86	1204.48	81.17	261.11	17.60	17.47	1.18	0.80	0.05
2002	1654.21	1352.20	81.74	274.57	16.60	26.53	1.60	0.90	0.05
2003	1905.21	1578.97	82.87	281.33	14.77	43.85	2.30	1.06	0.05
2004	2194.35	1810.38	82.50	330.99	15.08	50.47	2.30	2.51	0.11
2005	2497.53	2043.73	81.83	396.40	15.87	53.09	2.13	4.31	0.17
2006	2849.86	2374.15	83.31	414.77	14.55	54.84	1.92	6.09	0.21
2007	3264.40	2720.66	83.34	471.35	14.44	62.86	1.93	9.52	0.29
2008	3451.01	2803.00	81.22	565.55	16.39	69.22	2.01	13.25	0.39
2009	3681.19	3011.69	81.81	571.68	15.53	70.05	1.90	27.77	0.75
2010	4227.77	3416.89	80.82	686.74	16.24	74.74	1.77	49.40	1.17

Table 1 shows China's power structure, thermal power generation was more than 80% of the total generating capacity, and the generating capacity increased year by year; hydropower generating capacity maintains constant proportion of total generating capacity at 14.44-17.77%, and nuclear power generation has been very small proportion of the total generating capacity, the highest being 2.30% in year 2003 and 2004, others such as wind power, etc. is minimal. Hydropower has almost zero carbon emissions, nuclear chain greenhouse gas emissions is equivalent to 13.71g CO<sub>2</sub> (kwh)<sup>-1</sup>, while the coal chain greenhouse gas emissions is equivalent to 1302 g CO<sub>2</sub> (kwh)<sup>-1</sup> [3]. Thermal power is basically dominated by coal generation, meantime, the generators tend to have a longer service life, which implies that China's power industry has a strong carbon lock-in effect, that is the power industry CO<sub>2</sub> emissions will be "locked" by the current power structure in the future for a long period of time [4,5]. That is, the power system of carbon emissions will be mainly from thermal power generation. So in this paper, load forecast of power system for the next few years based on coal power load data for each year, and then carbon emissions of power system can be calculated according to the coal consumption.

## RESULTS AND DISCUSSION

Bases on the data of the power load in 2000-2010, according to the above method predicted power load for several years in the future. Taking into account the power system of carbon emissions mainly from thermal power, in this paper, we select the thermal power data.

Thermal power predictive value using Grey-Markov method

According to the aforementioned gray model GM (1,1), take the Thermal power data in 2000-2010 as the original sequence for grey prediction, forecast values as follows:

**Table 2: Thermal power predictive value**

Year	Generating capacity (billion kwh)	Year	Generating capacity (billion kwh)
2000	1107.92	2006	2253.10
2001	1304.44	2007	2513.35
2002	1455.11	2008	2803.65
2003	1623.18	2009	3127.48
2004	1810.67	2010	3488.72
2005	2019.81		

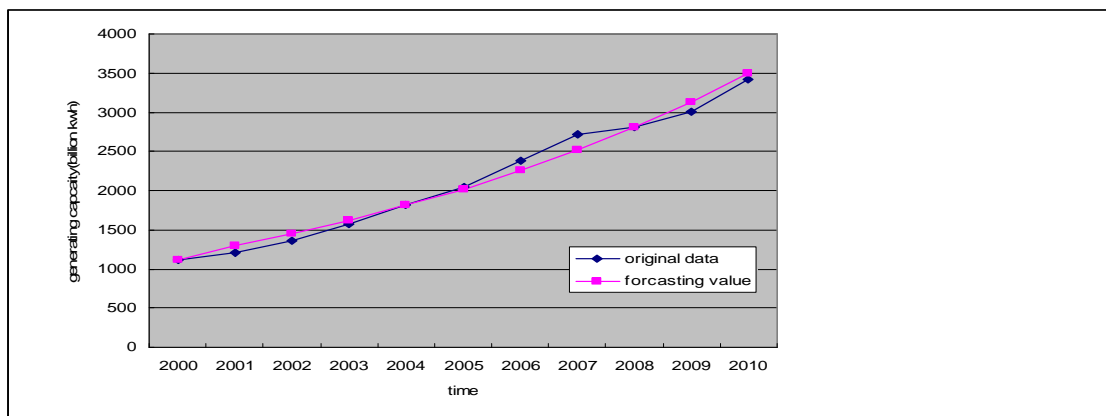


Fig.1: Original data compared with predicted values in 2000-2010

According to the aforementioned method, divide the status of forecasting values in 2000-2010

Table 3: Divide the status of gray forecasting values

Year	Actual value (billion kwh)	Forecasting value (billion kwh)	Residuals	Residuals proportion (%)	Status
2000	1107.92	1107.92	0	0	2
2001	1204.48	1304.44	-99.96	-8.30	1
2002	1352.20	1455.11	-102.91	-7.61	1
2003	1578.97	1623.18	-44.21	-2.80	2
2004	1810.38	1810.67	-0.29	-0.02	2
2005	2043.73	2019.81	23.92	1.17	3
2006	2374.15	2253.10	121.05	5.10	4
2007	2720.56	2513.35	207.21	7.62	4
2008	2803.00	2803.65	-0.65	-0.02	2
2009	3011.69	3127.48	115.79	-3.84	2
2010	3416.89	3488.72	-71.83	-2.10	2

The frequency statistics of the status transition from residuals can be obtained by Table 4:

Table 4 Frequency statistics of the residuals status transition

	Status 1	Status 2	Status 3	Status 4
Status 1	1	1	0	0
Status 2	1	3	1	0
Status 3	0	0	0	1
Status 4	0	1	0	1
Total	10			

Determine the state transition probability matrix

State transition probability matrix from the residuals frequency statistics for status transition is:

$$P = \begin{pmatrix} 0.5 & 0.5 & 0 & 0 \\ 0.2 & 0.6 & 0.2 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0.5 & 0 & 0.5 \end{pmatrix}$$

According to Markov prediction model,  $s_1 = s_0 * P; s_2 = s_0 * P^2; \dots; s_n = s_0 * P^n$ , It can be obtained the state transition forecasting value of 2020, 2030, 2040, 2050.

$$S_0 = (0.182 \quad 0.545 \quad 0.091 \quad 0.182)$$

$$\text{Final predictive value is: } V' = V(1 + P \times M)$$

In the formula,  $V'$  is the final predictive value,  $V$  is the gray predictive value,  $P$  is the largest probability value of the annual status,  $M$  is the median,  $M = 0.5 \times (U + L)$ ,  $U$  is the upper limit of the status,  $L$  is the lower limit of the status. Among them, the states 1 and 4 take directly -2% and 2%. So it can be obtained the load forecasting values: 2020 is 10504.67 billion kwh, 2030 is 31372.60 billion kwh, 2040 is 93620.31 billion kwh, 2050 is 279556.99 billion kwh.

#### Coal consumption values forecast

Most coal-power chain carbon emissions come from power generation. The major factor that impacts carbon emissions of power plants is coal consumption level. Its level is directly related not only to carbon emissions of the power plant, but also the coal-power chain carbon emissions. In recent years, a large number of old and small thermal powers were eliminated in China. Therefore, coal-fired power plants had a certain decline in coal consumption. the specific data are showed in table below. However, compared with developed countries China's has a long way to go until the problem of coal consumption is solved. But coal consumption trends and technological innovations in China show that coal consumption of China can be greatly declined in the future.

**Table 5 Coal consumption data 1970-2010**

Year	Coal consumption(g/kwh)	Year	Coal consumption(g/kwh)
1970	502	2002	383
1975	489	2003	380
1978	471	2004	376
1980	448	2005	374
1985	431	2006	366
1990	427	2007	356
1995	412	2008	349
2000	392	2009	342
2001	385	2010	333

Based on the above data, using the improved GM (1.1), that is gray rolling forecast, prediction results can be obtained as follows: 2020 is 293.822g/kwh, 2030 is 253.068g/kwh, 2040 is 217.968g/kwh, 2050 is 187.736g/kwh.

#### Calculation of power system carbon emissions

When power plant is in operation, It produced greenhouse gases mainly CO<sub>2</sub> and a small amount of N<sub>2</sub>O. NO<sub>x</sub> is generated by conventional combustion mode in coal-fired power plants, NO accounted for about 90%, N<sub>2</sub>O accounts for only about 1% [6]. According to the recommended values by National Development and Reform Commission Energy Research Institute and the Energy Handbook 2006, One ton of standard coal's CO<sub>2</sub> emission coefficient (t / tce) is 2.4567tCO<sub>2</sub>/tce, One ton of standard coal's NO<sub>x</sub> emission coefficient (t / tce) is 0.0156tNO<sub>x</sub>/tce. In addition, according to the greenhouse gases GWP default given by IPCC Third Assessment Report (2001), CO<sub>2</sub> is 1gCO<sub>2</sub> equivalent / g greenhouse gases, N<sub>2</sub>O is 296 gCO<sub>2</sub> equivalent / g greenhouse gases. Carbon emissions each year can be obtained by calculating. The result is: the CO<sub>2</sub> emission of 2020 is 7.7254 billion tons, 2030 is 20.0616 billion tons, 2040 is 51.0740 billion tons, 2050 is 131.3582 billion tons.

According to China's power industry development characteristics and the characteristics of primary energy, the most effective measures of CO<sub>2</sub> emission reduction is to adjust the industrial structure. That is, orderly and vigorously develop hydropower, wind and solar clean energy generation under the premise of protection of environment. Substituting hydropower, wind power and solar power for thermal power can bring a decrease of CO<sub>2</sub> emissions about 1kg per kwh, thus low-carbon benefits are obvious. Developing such energy plays an important role in achieving the development of low-carbon electricity in China. According to our calculations, for example, if the proportion of thermal power generation of total generated energy decrease by 20% in 2050, the CO<sub>2</sub> emissions would be reduced by about 26 billion tons. However, clean energy also has a series of problems to be solved, including higher cost and higher demands of corresponding supporting of electricity grid and cost requirements. Development of large-scale clean energy power will cause a large increase of cost burden to power plants.

In addition, another way for the power system to reduce carbon emissions is to reduce coal consumption. Currently, China's coal units are mainly using ultra units and subcritical unit, which are typical examples of efficient power generation technology, therefore there is considerable space to improve the coal utilization efficiency and reduce carbon emissions. For example, if the coal consumption is decreased by 1g/kwh, CO<sub>2</sub> emissions would be reduced by about 0.7 million tons in 2050. Meanwhile, intending to reduce carbon emissions, there are two trends of development of coal power generation technology outside China: improving power generation efficiency and recycling coal boilers, gas and steam boiler. The typical example of the former is Supercritical units (SC) and Ultra-supercritical units (USC) power generation technology, of the latter is mainly Integrated Gasification

Combined Cycle (IGCC) power generation technology. These techniques really applied to power generation need some time and effort.

### CONCLUSION

The results showed that: CO<sub>2</sub> emissions from the power system have a rising trend. If the existing power structure is kept, emission reduction works of power systems will have a long way to go. To construct of low-carbon electricity system, not only the existing fossil fuel generators need to reduce emissions, but also renewable energy and other clean energy will be relied on in the long term. So we can work from the following aspects.

On the level of the national policy, we can levy "carbon tax" timely and at appropriate which tax will be able to be internalize the external costs of the greenhouse gas emissions directly and effectively. It will be of great benefit to settle the long-term environmental problems. We can also establish and improve the carbon market. Carbon trading market will change with prices and supply-demand changes in the overall operation, but there are many issues in the implementation of the carbon trading market that need further study. Government departments need to establish the industry's carbon emissions targets and strictly supervise execution. Implement differential pricing to different power plants to encourage the implementation of low-carbon electricity, and also introduce some incentive measures to promote energy conservation and emission reduction to small and medium enterprises.

On the level of power generation components encourage the low-carbon development of power generation enterprises, increase low-carbon technology innovation and application of fossil fuel in power generation, the development of recycling economy; adjust carbon structure appropriate, develop renewable energy vigorously, increase nuclear power and hydropower proportion appropriate.

On the level of the power grid optimize the layout of power plants and power grid, increase the smart power grid construction; strengthen low-carbon electricity scheduling constraints; continue to build UHA substation and digital substation.

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