



Research Article

ISSN : 0975-7384
CODEN(USA) : JCPRC5

Cluster analysis of players category classification in 2013 NBA all-star game based on SPSS

Dawei Shi

Department of Physical Education, Hebei University of Technology, Tianjin, China

ABSTRACT

NBA all-star game is a game that attracts tremendous attentions. The competitiveness that starts show in the game leads the development of world basketball techniques, while the key factor indicates competitiveness is sport technical index features and so more scientific analysis of techniques and tactics level in all-star game is a researchable topic. This paper adopts cluster analysis from SPSS and Fisher discriminate analysis method to make category classification to 24 players in 2013 NBA all-star game, and analysis of techniques and tactics index after quantization so as to explore the key for getting victory in competition and basis of techniques and tactics level playing through data concentration effect. At first, this paper makes research on technical index data that offered by officials in NBA game, and carries out standardization handling with such data, then discusses application range of cluster analysis and rationality that basketball techniques and tactics level reflect in detail, finally utilize cluster analysis method to analyze index level that stars respectively in eastern and western conference show in the game, gets NBA stars classification result according to index level to provide data basis for selecting targeted players' tracking on NBA key players techniques research.

Key words: Cluster analysis, techniques and tactics index, data standardization, SPSS mathematical statistics

INTRODUCTION

In the rapid and comprehensive development of modern basketball, outcome of basketball game is up to many factors, but the decisive factor reflects in the balance of power between two parties including techniques, tactics, willpower, players' physical conditions as well as psychological quality and competition experiences so on. Make classification of players is needed to extract different categories of players and implement technical motions tracking on them, therefore classification according to data features of technical index can get comprehensive and scientific category.

There are many methods for classification according to technical index data for players. For cluster analysis and Fisher discriminant analysis researching, lots of people have made efforts and applied that into category classification fields. Among them, Zhang Dan Utilize SPSS software to do research on basketball qualitative data and extend qualitative analysis method in physical education field application [1]; Xiong Feng-Mei Make cluster analysis of NBA players' cost performance, firstly divide them into 4 categories then classify them with their compensation level, divide them into the most efficiency, higher efficiency, normal efficiency, low efficiency players and suggest team to mine for value players and exclude deficient players when renewal of a contract with players [2]; Yuan Li-Huang Apply linear probability model to analyze then influence factors for NBA games outcome, get that positive factors that effect on NBA game result including defensive rebound numbers, assist times, steal times and so on. Main negative influence factor is fault times [3].

This paper analyzes technical index data produced from stars in 2013 NBA all-star game so as to make scientific and

rational classification to players through cluster analysis and Fisher discriminant analysis method, and provide data basis and theoretical foundation for targeted players tracking.

NBA OFFICIAL INDEX DATA STANDARDIZATION AND ANALYSIS METHOD THEORETICAL BASIS NBA official index quantification and data standardization

NBA official statistics technical indexes including players' height, score, field-goal percentage, rebound, assist, steal, blocked shot and fault, players indexes statistics in eastern conference and western conference as Table 1 shows.

Table1: Eastern conference and western conference technical index statistics in 2013

No.	player	height	score	Field-goal percentage	rebound	assist	steal	Blocked shot	fault
eastern conference									
1	Lebron James	2.03	19	38.89%	3	5	1	0	4
2	Chris Bosh	2.08	6	33.33%	2	1	1	0	3
3	Dwane Wade	1.93	21	76.92%	3	7	2	2	4
4	Kevin Garnett	2.12	0	0.00%	3	1	0	0	1
5	Carmelo Anthony	2.03	26	57.14%	12	3	0	0	1
6	Jrue Holiday	1.93	6	50.00%	2	1	2	0	1
7	Paul George	2.03	17	53.85%	3	4	2	0	0
8	Tyson Chandler	2.16	7	40.00%	8	0	0	0	0
9	Brook Lopez	2.13	3	0.00%	5	3	0	0	1
10	Kyrie Irving	1.91	15	54.55%	3	4	0	0	2
11	Joakim Noah	2.11	8	57.14%	10	3	0	1	1
12	Luol Deng	2.06	10	40.00%	2	1	0	0	2
western conference									
1	Dwight Howard	2.11	9	66.67%	7	0	0	0	1
2	Kevin Durant	2.06	30	54.17%	6	1	2	0	0
3	Kobe Bryant	1.98	9	44.44%	4	8	2	2	1
4	Blake Griffin	2.06	19	81.82%	3	3	2	1	0
5	Chris Paul	1.83	20	70.00%	0	15	4	0	3
6	Tony Parker	1.88	13	50.00%	1	5	2	0	3
7	Russell Westbrook	1.91	14	53.85%	4	3	1	0	2
8	David Lee	2.06	6	75.00%	2	0	2	0	1
9	Zach Randolph	2.06	6	50.00%	5	0	0	0	0
10	Tim Duncan	2.11	2	25.00%	3	0	0	0	1
11	James Harden	1.93	15	46.15%	6	3	0	0	2
12	LaMarcus Aldridge	2.11	0	0.00%	4	1	0	2	1

Due to measurement of index selection would direct effect on the result of cluster analysis, normally the smaller the measurement unit chosen, the bigger the variable value would be, the larger influence on cluster result would be. In order to avoid dependency to variable unit selection, data should be done standardization. When data dimension is different, standardization should be implemented, but data dimension is same while order of magnitude has great difference, standardization should also be done. Data standardization method adopted in this paper is standard deviation standardization method, average value of data after standardization is 0, and standard deviation is 1 so as to eliminate dimension influence [4,5]. When samples change, their data after standardization still keep relative stability. Data standardization formula is as formula (1) shows.

$$x_{ij}^* = \begin{cases} \frac{x_{ij} - \bar{x}_j}{s_j} & s_j \neq 0 \\ 0 & s_j = 0 \end{cases} \begin{matrix} (i = 1, 2, \dots, n) \\ (j = 1, 2, \dots, m) \end{matrix} \quad (1)$$

In formula(1), x_{ij}^* represents sample value after standardization, x_{ij} represents sample value, \bar{x}_j represents average value of one selected index sample, s_j represents sample data standard deviation.

Cluster analysis method theoretical basis

Cluster analysis is also called group analysis, is a multivariate statistics method to classify samples or indexes, which makes category classification of similar elements, it can divide into two kinds as sample cluster and variable cluster according to difference of classification objects [6].

Sample cluster is called Q cluster in statistics, that is cluster observed quantity in SPSS terms, it clusters each variable value that reflect observed objects features according to observed objects each feature; Variable cluster is called R cluster. Since many variables reflect the same thing features, partial variables are chosen to make research on one aspect of thing according to problems that research. Due to human have limited recognition of objective

things, normally is difficult to find typical variables that independent from each other so that affect problems' further recognition and research. Therefore, it usually starts with variable cluster, and then finds out independent variable which is independent and typical so as to achieve effect without losing most information.

In order to make scientific classification of samples or indexes, relationship among samples should be researched. By far the most widely used two methods are similarity factor and spatial distance. From which the bigger similarity factor is, its nature more closely to samples, then classify the similar sample into one category; while bigger spatial distance means its nature quite further from samples, it can classify it into one category which distance becomes smaller. Common distances are like Ming distance as formula (2) shows, mahalanobis distance as formula (3) shows and lance distance as formula (4) shows, and common similarity factors are like included angle cosine as formula(5) shows and correlation index as formula(6)shows.

$$d_{ij}(q) = \left(\sum_{a=1}^p |x_{ia} - x_{ja}|^q \right)^{\frac{1}{q}} \quad (2)$$

$$d_{ij}^2(M) = (X_i - X_j)' \Sigma^{-1} (X_i - X_j) \quad (3)$$

In formula(3), Σ represents index covariance matrix.

$$d_{ij}(L) = \frac{1}{p} \sum_{a=1}^p \frac{|x_{ia} - x_{ja}|}{x_{ia} + x_{ja}}, i, j = 1, 2, \dots, n \quad (4)$$

$$\cos \theta_{ij} = \frac{\sum_{a=1}^p x_{ia} x_{ja} X_i}{\sqrt{\sum_{a=1}^p x_{ia}^2 \cdot \sum_{a=1}^p x_{ja}^2}}, -1 \leq \cos \theta_{ij} \leq 1 \quad (5)$$

$$r_{ij} = \frac{\sum_{a=1}^p (x_{ia} - \bar{x}_i)(x_{ja} - \bar{x}_j)}{\sqrt{\sum_{a=1}^p (x_{ia} - \bar{x}_i)^2 \cdot \sum_{a=1}^p (x_{ja} - \bar{x}_j)^2}}, -1 \leq r_{ij} \leq 1 \quad (6)$$

This paper mainly adopts the special condition that $q = 2$ in Ming distance, that is square Euclidean distance, as formula (7) shows.

$$d(x, y) = \sum_i (x_i - y_i)^2 \quad (7)$$

Discriminant analysis method theoretical basis

Discriminant analysis is a statistics method that discriminate samples category, it is different from cluster analysis that establishes discriminant with some criterion based on some categories that research objects already being divided and acquired each category one batch known samples observed data, and then make discriminant classification to unknown samples.

Discriminant analysis is rich in content and multiple in method. Classify according to discriminant groups, it can be divided into two groups discriminant analysis and multiple groups discriminant analysis; according to mathematical models distinguish different total, it can be divided into linear discriminant and non linear discriminant; according to different variable handling methods in discriminant, it can be divided into step discrimination and discriminant tree etc. Among them, distance discriminant analysis is a common discriminant method, its basic idea is first respectively calculate each category gravity center according to classification data, the discriminant criterion is judge one as it comes from i category when it arrives the nearest to i category gravity center distance by one observation; Given two totals to be G_1, G_2 , take n_1 samples from G_1 , take n_2 samples from G_2 , and measure P indexes of each sample, acquire one sample actual measurement index value as $X = (x_1, x_2, \dots, x_p)'$ at random; to judge which category that X belongs to, distance between X and totals of G_1 and G_2 should be firstly

calculated, and respectively mark them as $D(X, G_1)$, $D(X, G_2)$, make discriminant classification according to nearest distance criterion and write it down as formula (8) shows.

$$\begin{cases} X \in G_1, D(X, G_1) < D(X, G_2) \\ X \in G_2, D(X, G_1) > D(X, G_2) \\ \text{To be discrim, } D(X, G_1) = D(X, G_2) \end{cases} \quad (8)$$

In formula(8), To be disc rim represents To be discriminant that is the meaning of waiting to be discriminated.

This paper adopts Fisher discriminant method, this method is select discriminant function with the standard of Fisher criterion, which refers to relative good discriminant function can make distinguish its own category from others according to be discriminant objects n indexes to the largest extent.

Fisher discriminant method is first integrate multiple dimensional variable X each index into one dimensional index Y and establish linear discriminant function, then make distance discriminant to one dimensional variable Y , which actually is a dimensionality reduction. Normal form of linear discriminant function is as formula (9) shows.

$$Y = a_0 + a_1X_1 + a_2X_2 + \dots + a_nX_n \quad (9)$$

In formula(9), Y represents discriminant fraction, X_i represents variable that reflects research objects characteristics, a_i represents characteristic variables discriminant index.

EMPIRICAL RESULT ANALYSIS

Result after data standardization

NBA all-star game official technical index statistics data in 2013 after standardization is as Table 2 shows.

Table 2: Technical index data standardization of eastern conference and western conference in 2013

No.	player	height	score	Field-goal percentage	rebound	assist	steal	Blocked shot	fault
eastern conference									
1	Lebron James	-0.159	0.941	-0.125	-0.487	1.097	0.376	-0.402	1.702
2	Chris Bosh	0.438	-0.690	-0.389	-0.780	-0.854	0.376	-0.402	0.973
3	Dwane Wade	-1.354	1.192	1.548	-0.487	2.073	1.502	2.815	1.702
4	Kevin Garnett	0.916	-1.443	-1.841	-0.487	-0.854	-0.751	-0.402	-0.486
5	Carmelo Anthony	-0.159	1.819	0.668	2.144	0.122	-0.751	-0.402	-0.486
6	Jrue Holiday	-1.354	-0.690	0.360	-0.780	-0.854	1.502	-0.402	-0.486
7	Paul George	-0.159	0.690	0.536	-0.487	0.610	1.502	-0.402	-1.216
8	Tyson Chandler	1.394	-0.565	-0.081	0.975	-1.341	-0.751	-0.402	-1.216
9	Brook Lopez	1.035	-1.066	-1.841	0.098	0.122	-0.751	-0.402	-0.486
10	Kyrie Irving	-1.593	0.439	0.580	-0.487	0.610	-0.751	-0.402	0.243
11	Joakim Noah	0.797	-0.439	0.668	1.559	0.122	-0.751	1.207	-0.486
12	Luol Deng	0.199	-0.188	-0.081	-0.780	-0.854	-0.751	-0.402	0.243
Average value		2.0433	11.500	0.4183	4.6667	2.7500	0.6667	0.2500	1.6667
Standard deviation		0.0084	7.9715	0.2272	3.4201	2.0505	0.8876	0.6216	1.3707
Western conference									
1	Dwight Howard	1.033	-0.345	0.683	1.552	-0.733	-0.971	-0.526	-0.237
2	Kevin Durant	0.525	2.141	0.124	1.074	-0.508	0.582	-0.526	-1.185
3	Kobe Bryant	-0.288	-0.345	-0.315	0.119	1.071	0.582	1.997	-0.237
4	Blake Griffin	0.525	0.839	1.359	-0.358	-0.056	0.582	0.736	-1.185
5	Chris Paul	-1.812	0.957	0.831	-1.791	2.650	2.135	-0.526	1.658
6	Tony Parker	-1.304	0.128	-0.064	-1.313	0.395	0.582	-0.526	1.658
7	Russell Westbrook	-0.999	0.247	0.110	0.119	-0.056	-0.194	-0.526	0.711
8	David Lee	0.525	-0.700	1.055	-0.836	-0.733	0.582	-0.526	-0.237
9	Zach Randolph	0.525	-0.700	-0.064	0.597	-0.733	-0.971	-0.526	-1.185
10	Tim Duncan	1.033	-1.174	-1.183	-0.358	-0.733	-0.971	-0.526	-0.237
11	James Harden	-0.796	0.365	-0.234	1.074	-0.056	-0.971	-0.526	0.711
12	LaMarcus Aldridge	1.033	-1.411	-2.301	0.119	-0.508	-0.971	1.997	-0.237
Average value		2.0083	11.917	0.5143	3.7500	3.2500	1.2500	0.4167	1.2500
Standard deviation		0.0984	8.447	0.2235	2.0944	4.4339	1.2881	0.7930	1.0553

Cluster analysis result

Apply SPSS19.0 to cluster analysis of eastern conference 12 players and western conference 12 players, get results as Table 3, Table 4 and Figure 1 show.

Table 3: Case handling summarize

valid		loss		total	
N	percentage	N	percentage	N	percentage
24	100.0	0	.0	24	100.0

a. square Euclidean distance already used; b. Ward join

Table 4: Table of Ward joins cluster members

cluster member	5 cluster	4 cluster	3 cluster	cluster member	5 cluster	4 cluster	3 cluster
Lebron James	G1	G1	G1	Dwight Howard	G5	G4	G3
Chris Bosh	G2	G1	G1	Kevin Durant	G5	G4	G3
Dwane Wade	G3	G2	G2	Kobe Bryant	G2	G1	G1
Kevin Garnett	G4	G3	G3	Blake Griffin	G2	G1	G1
Carmelo Anthony	G5	G4	G3	Chris Paul	G3	G2	G2
Jrue Holiday	G2	G1	G1	Tony Parker	G1	G1	G1
Paul George	G2	G1	G1	Russell Westbrook	G1	G1	G1
Tyson Chandler	G5	G4	G3	David Lee	G2	G1	G1
Brook Lopez	G4	G3	G3	Zach Randolph	G5	G4	G3
Kyrie Irving	G1	G1	G1	Tim Duncan	G4	G3	G3
Joakim Noah	G5	G4	G3	James Harden	G1	G1	G1
Luol Deng	G2	G1	G1	LaMarcus Aldridge	G4	G3	G3

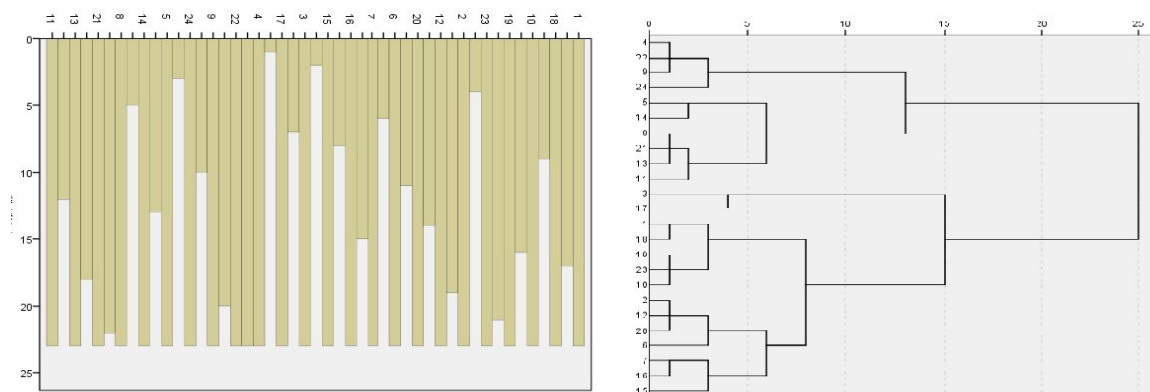


Figure 1: Cluster numbers vertical dendrogram and Ward joins tree diagram

According to SPSS19.0 operation result, it can be known that total 24 players from eastern and western conference can be divided into 4 categories according to official offered index data as following.

First category, eastern conference's Lebron James, Chris Bosh, Jrue Holiday, Paul George, Luol Deng and Kyrie Irving; Western conference's Kobe Bryant, Tony Parker, Blake Griffin, Russell Westbrook, David Lee and James Harden;

Second category, eastern conference's Dwane Wade and western conference's Chris Paul;

Third category, eastern conference's Kevin Garnett and Brook Lopez, western conference's Tim Duncan and LaMarcus Aldridge;

Fourth category, eastern conference's Carmelo Anthony, Tyson Chandler and Joakim Noah, western conference's Dwight Howard, Kevin Durant and Zach Randolph.

Fisher criterion discriminant result

Use SPSS to divide eastern and western conference players into 4 categories, four linear discriminant functions should be established, when makes discriminant of each individual, leads test participants each variable value into discriminant function, and gets discriminant scores so that can define category that individuals belong to.

According to preliminary classification result got in 2.2, then based on 4 categories results vectors by cluster analysis, defined new variable "grouping category" choose SPSS-->analysis-->classification-->discriminant, adopts independent variable fully entering model to implement discriminant analysis, therefore variable value range is from 1 to 4. According to operation result, it can get each index Fisher linear index and constant in 4 categories grouping as Table 5 shows.

Table 5: Table of classification function index

statistical index	group1 index	Group 2 index	Group 3 index	Group 4 index
height	-3.959	13.292	-19.052	10.444
score	1.363	-1.896	-0.049	0.540
Field-goal percentage	-1.489	3.399	-3.179	1.410
rebound	-3.371	6.372	-8.417	6.381
assist	-2.578	0.988	3.440	-1.464
Steal	-.0470	2.081	-3.232	1.067
blocked shot	-.0830	0.815	2.304	-3.650
fault	2.420	-5.838	7.315	-4.380
constant	-3.965	-14.814	-25.282	-10.146

Cluster result of NBA eastern and western conference players belong as Table 6 show.

Table 6: Table of Fisher criterion discriminant result

Cluster member	Cluster1	Cluster2	Cluster 3	Cluster 4	affiliation	Cluster member	Cluster1	Cluster2	Cluster 3	Cluster 4	affiliation
Lebron James	1.0813	-30.637	-3.7200	-21.775	G1	Dwight Howard	-13.368	9.9917	-62.509	14.3177	G4
Chris Bosh	1.1411	-20.046	-23.753	-12.613	G1	Kevin Durant	-8.4722	2.5685	-58.332	11.9962	G4
Dwane Wade	0.8273	-35.381	20.8465	-43.730	G3	Kobe Bryant	-6.7548	-13.019	-15.107	-20.222	G1
Kevin Garnett	-4.0812	-9.1603	-37.703	-3.0170	G4	Blake Griffin	-8.5284	1.5853	-45.678	-1.3712	G2
Carmelo Anthony	-10.500	-3.3768	-44.146	6.4145	G4	Chris Paul	6.4372	-52.348	34.7585	-45.754	G3
Jrue Holiday	3.5366	-30.458	-6.3045	-22.681	G1	Tony Parker	8.9038	-49.480	21.2047	-37.463	G3
Paul George	-6.1040	-9.0172	-32.469	-6.2828	G1	Russell Westbrook	1.6795	-32.467	-3.1890	-20.851	G1
Tyson Chandler	-12.837	14.6073	-71.769	18.1704	G4	David Lee	-4.4179	-6.8077	-38.915	-4.2358	G4
Brook Lopez	-8.5266	-3.6014	-41.555	0.7335	G4	Zach Randolph	-9.8035	0.8225	-49.334	5.8256	G4
Kyrie Irving	2.8022	-40.659	12.6786	-30.127	G3	Tim Duncan	-5.2811	-6.9496	-40.460	-0.9487	G4
Joakim Noah	-15.524	11.1952	-53.618	5.5739	G2	James Harden	-1.6339	-26.693	-11.495	-13.887	G1
Luol Deng	0.5992	-21.211	-21.901	-12.409	G1	LaMarcus Aldridge	-6.3368	-4.9823	-34.322	-9.1477	G2

CONCLUSION

Through Table 2 and Table 6, it can be known the NBA stars index classification contrast condition by 2 methods, as Table 7 shows.

Table 7: Result of NBA stars index classification by different methods

Cluster member	Cluster result	Discriminant result	Result comparison	Cluster member	Cluster result	Discriminant result	Result comparison
Lebron James	G1	G1	√	Dwight Howard	G4	G4	√
Chris Bosh	G1	G1	√	Kevin Durant	G4	G4	√
Dwane Wade	G2	G3	×	Kobe Bryant	G1	G1	√
Kevin Garnett	G3	G4	×	Blake Griffin	G1	G2	×
Carmelo Anthony	G4	G4	√	Chris Paul	G2	G3	×
Jrue Holiday	G1	G1	√	Tony Parker	G1	G3	×
Paul George	G1	G1	√	Russell Westbrook	G1	G1	√
Tyson Chandler	G4	G4	√	David Lee	G1	G4	×
Brook Lopez	G3	G4	×	Zach Randolph	G4	G4	√
Kyrie Irving	G1	G3	×	Tim Duncan	G3	G4	×
Joakim Noah	G4	G2	×	James Harden	G1	G1	√
Luol Deng	G1	G1	√	LaMarcus Aldridge	G3	G2	×

According to discriminant result comparison, it can be known that total 13 players affiliated cluster result is the same as their discriminant result, which indicates the directivity of discriminant classification result is correct to some extent, so final classification result should follow result in Table 6.

REFERENCES

- [1] Deng Weiming, Sun Xuechuan, Fan Xiaoyan, JIAN Gun lin. *Journal of Physical Education*, **2003**, 10(1), 47-49.
- [2] Gong Ming-bo, Zhong Ping. *China Sport Science*, **2005**, 25(1), 87-90.

- [3] Deng Wei-ming, Sun Xue-chuan. *Journal of Physical Education*, **2006**, 13(4), 63-65.
- [4] Zheng Qi. *Journal of Physical Education*, **1998**, (1).
- [5] Zhang Li, MA Wei-min. *Journal of Physical Education*, **2006**, 13(1), 68-71.
- [6] Bing Zhang, Sheng Zhang and Guang Lu. *Journal of Chemical and Pharmaceutical Research*, **2013**, 5(9), 256-262.