



## Application of BP neural network in predicting the cement materials performance

Deng Xue-jie<sup>\*</sup>, Kang Tao and Wang Dong-sheng

<sup>1</sup>School of Mines, China University of Mining & Technology, Xuzhou, Jiangsu, China

<sup>2</sup>Key Laboratory of Deep Coal Resource Mining, Ministry of Education of China, China University of Mining and Technology, Xuzhou, Jiangsu, China

---

### ABSTRACT

The 4-10-5 prediction network model was established based on the improved BP neural network, considering that the performance of cement materials are impacted by many factors and the multivariate cross of those factors are difficult and strenuous to study in laboratory. Furthermore, the network model was trained and tested with the data collected from the laboratory test results. The results showed that the prediction precision of the well trained network model is high and reliable, whose fitting correlation coefficient and average prediction error are 0.969 and 6.72% respectively. Finally, the well trained network model was applied to predict the optimal material ratio, which can meet the requirement. Specifically, the optimal material ratio of fly ash, quicklime, cement, and gangue in cement materials are 35%, 10%, 2%, and 53% respectively, and the concentration of slurry is 77% by the above proportion. The cemented backfilling materials under this ratio has good effect in field application which prove the reliable of this prediction model.

**Keywords:** cemented backfilling materials; material ratio; performance prediction; BP neural network; Matlab toolbox

---

With the development of mining technology, "Green Mining" has become the future trend. The backfilling mining technology is an important way to achieve the "Green Mining"<sup>[1-3]</sup>. Among the numerous backfilling mining technologies, the cemented backfilling mining technology is an effective method, which is based on the gangue and fly ash as the main filling materials. In this method, the backfilling slurry is made from a certain proportion of gangue, fly ash and cementing materials. The slurry is made with no need for dewatering process and then piped to the underground by using the filling pump to fill the gob timely<sup>[4]</sup>. Cement materials is the core of cemented backfilling mining technology and their properties, such as slump, bleeding rate, different age strength, etc. are the key to the successful applications of the technology. The performance of Cement materials are impacted by many factors<sup>[6-7]</sup> including not only established and quantifiable factors, but also some uncertain or obscure factors, which is of complex non-linear relationship between them<sup>[8]</sup>. In order to study the performance of cemented filling materials under different influence factors, many scholars have mainly conducted the tests in laboratory. However, most research to date only focus on single-factor<sup>[9-11]</sup> and unable to have comprehensive analysis of multivariate cross which need a large amount of labor and have puzzled engineers on mining production decisions in field applications<sup>[12]</sup>.

BP neural network (BPNN) is one of the most widely used neural network model which is one kind of multilayer feed forward network trained by error back-propagation algorithm<sup>[13]</sup>. The network model can achieve nonlinear mapping between the input samples and the output samples, and it has features of self-organizing and self-learning that make it effective at nonlinear approximation. Moreover, the underlying relationship between those data can be induced through learning process of its own accord<sup>[14-15]</sup>. Therefore, the BPNN is apparently effective in predicting the performance of cemented filling materials, such as Zhou Huaqiang, Chang Qingliang, Wei Wei and other scholars

have done those related research, but only built a network model with one single output for one performance of the materials<sup>[7-8]</sup>. In order to solve the problem of poor speed of converging and easy to fall into local minimum in the application of standard BPNN model, the additional momentum and self-adaptive learning rate are introduced to improved BP network standard algorithm<sup>[8]</sup>. The improved network is of stronger mapping capabilities, higher network training speed and avoiding falling into local minimum.

In this paper, the performance of cement materials is obtained by laboratory test on different materials ratio. Based on the improved BPNN, the prediction model with multi-input and multi-output is established to predict the performance of cemented filling materials, whose structure is 4-10-5. Specifically, the slump, bleeding rate, 3d, 7d and 28d age strength can be predicted under different concentration, fly ash, quicklime and cement consumption. And the model was trained and tested by laboratory data with Matlab 7.1 platform and then it was applied in Gonggayingzi coal mine. The results show that the precision of prediction is high and reliable and meets the needs of production practice.

## 1 Improved BPNN model<sup>[13]</sup>

### 1.1 Additional momentum method

Based on back-propagation method, a value which is proportional to the previous weight variation is added to each current weight variation, then a new weight variation is obtained. The weight adjustment formula with additional momentum factor are as follows.

$$\begin{aligned}\Delta w_{ij}(k+1) &= (1 - mc)\eta\delta_i p_j + mc\Delta w_{ij}(k) \\ \Delta b_i(k+1) &= (1 - mc)\eta\delta_i + mc\Delta b_i(k)\end{aligned}\quad (1)$$

Where

$k$  is the number of training;

$mc$  is the momentum factor which is about 0.95 generally;

$\Delta w_{ij}(k+1)$  and  $\Delta w_{ij}(k)$  are the revised and the current weight difference respectively;

$\Delta b_i(k+1)$  and  $\Delta b_i(k)$  are the revised and the current threshold difference respectively;

$\eta$  is learning rate;

$\delta_i p_j$  and  $\delta_i$  are the current weight and the threshold gradient respectively.

### 1.2 Self-adaptive learning rate

Self-adaptive learning rate can ensure that the network is always training at the maximum acceptable learning rate. The learning rate will reduce when a new error exceeds a certain multiple of the old one, otherwise the learning rate remain stable. On the other hand, the rate will increase when a new error is smaller than the old one. An adjustment method of adaptive learning rate is shown in formula (2).

$$\eta(k+1) = \begin{cases} 1.05\eta(k), & SSE(k+1) < SSE(k) \\ 0.7\eta(k), & SSE(k+1) > 1.04 \cdot SSE(k) \\ \eta(k) & \end{cases}\quad (2)$$

Where

$\eta(k+1)$  and  $\eta(k)$  are the revised and the current learning rate respectively;

$SSE(k+1)$  and  $SSE(k)$  are the revised and the current variance respectively.

## 2 Cement materials laboratory testing

### 2.1 Composition of cement materials

According to the actual situation of coal production, cement materials are consisted of gangue, fly ash, quicklime, cement and water which mixed together in a reasonable proportion in which gangue acted as coarse aggregate, fly ash acted as fine aggregate, quicklime and a small amount of cement acted as binder.

The particle size of gangue are required no more than 25mm in order to achieve pumping and a long-distance pipelines transport of cement materials. The fly ash, whose diameter is 0.005~0.05mm, is mainly used to fill the gaps

between the coarse aggregate, in which the ultrafine grain size has a larger surface area and sufficient saturated aqueous. After combination with water molecules they distribute in the gaps between the aggregate, which ensure the workability and the stability of the solid particles on structure surface of the cemented filling materials. The calcium oxide takes 39% in quicklime, whose role is to stimulate the activity of quicklime to generate the hydraulic cementation material. The cement works as a lubricant in the process of filling material transportation and also increases the adhesion of the slurry during the solidification process, which ensure the filling body has a higher carrying capacity.

In order to test the components of material mineral in cemented backfilling materials, XRD method is used and the results of X-ray diffraction shown in Figure 1.

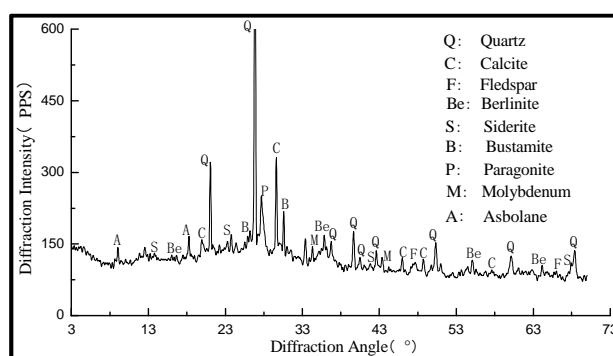


Fig1 X-ray diffraction pattern of cemented backfilling materials

Figure 1 shows that the main mineral composition of the cement materials are quartz, calcite, feldspar, berlinite and siderite, and it also contains small amounts of bustamite, paragonite, molybdenum and asbolite. The more content of quartz in materials leads to a higher bearing strength, and the calcite, feldspar mica, siderite and other materials are easy to bring hydrolysis and weathering phenomena to the materials.

## 2.2 Test ratio

The ratio of each component in cement material has a great influence on the performance of cement materials for they are made of a variety of materials. Therefore, the concentration of slurry, the proportion of fly ash, quicklime and cement are adjusted reasonably to test their corresponding performance. The specific ratio of test program are shown in Table 1.

Tab.1 Ratio of cement materials test

No. of ratio	Concentration of slurry /%	Dry percentage /%			
		Fly ash	Quicklime	Cement	Original gangue
1	73	40	10	2.5	47.5
2	74	40	10	2.5	47.5
3	75	40	10	2.5	47.5
4	76	40	10	2.5	47.5
5	77	40	10	2.5	47.5
6	75	30	10	2.5	57.5
7	75	35	10	2.5	52.5
8	75	45	10	2.5	42.5
9	75	50	10	2.5	37.5
10	75	40	6	2.5	51.5
11	75	40	8	2.5	49.5
12	75	40	12	2.5	45.5
13	75	40	14	2.5	43.5
14	75	40	10	0	50
15	75	40	10	1.5	48.5
16	75	40	10	3.5	46.5
17	75	40	10	5	45
18	74	35	10	2.5	52.5
19	76	40	10	0	50
20	77	40	12	2.5	54.5

## 2.3 Testing program

The test was concentrated on the transportation performance and the compressive strength of different ratio of cement materials.

(1) Test on the transportation performance of slurry

The test on the transportation of slurry are composed of the slump test and the bleeding rate test. Slump is a simple and intuitive reference index in engineering operations when pump cement materials, and its value directly reflects the flow state and the frictional resistance of cement materials. Bleeding is the phenomenon which coarse aggregates go down and water floats up during the transportation, vibration and pumping process of cement materials. And the phenomenon of segregation will be produced in the transportation process when the bleeding rate of slurry is too large, which lead to a pipe blockage. Both these tests refer to the *standards method in ordinary concrete mixture performance test* (GB/T 50080-2002).

(2) Test on the compressive strength of cement materials

The 70.7mm×70.7mm×70.7mm standard test cube is used as specimen. The specimen is moved to maintain under a standard conditions with the temperature 20±2°C and the relative humidity 95% after kept in the mould for 1d, Then kept in the mould for 3d, 7d and 28d in the same way to test their compressive strength.

In order to conduct the uniaxial compression test, SANS mechanics of materials testing machine was used with a load speed of 1mm/min. The uniaxial anti-compressive strength value was obtained by calculating the average value of 3 specimens taken from each group.

## 2.4 Testing result

The performance index of cement materials with different ratio were shown in Table 2 based on the above test.

Tab.2 testing result

No. of ratio	Slump /mm	Bleeding rate /%	Compressive strength/MPa		
			3d	7d	28d
1	245	3.95	0.52	0.77	1.27
2	240	3.84	0.61	0.86	1.65
3	230	3.44	0.71	1.22	1.83
4	165	2.95	0.85	2.13	2.91
5	150	2.09	0.96	2.65	3.2
6	237	3.9	0.67	1.39	1.58
7	200	3.8	0.71	1.56	1.65
8	152	1.73	0.95	1.92	2.49
9	143	1.66	0.83	1.67	2.04
10	226	3.68	0.53	1.08	1.55
11	205	3.55	0.73	1.25	1.77
12	168	1.88	0.82	1.69	2.92
13	154	1.75	0.65	1.46	2.72
14	205	2.67	0.58	0.74	0.8
15	217	2.64	0.66	1.16	1.64
16	220	2.65	0.85	1.28	1.73
17	200	2.67	0.96	1.35	1.91
18	247	3.86	0.65	0.98	1.46
19	165	2.41	0.62	1.39	1.74
20	150	1.84	1.05	2.27	3.33

## 3 Cement materials performance prediction model

### 3.1 Establishment of prediction model

It has been proved theoretically that the feed forward network with 3-layer can approximate any continuous function in any arbitrary precision and the feed forward network with deviation, at least one S hidden layer and one linear output layer can approximate any rational function<sup>[13]</sup>. Therefore, the network was determined to three layers, namely one input layer, one output layer and one hidden layer. Based on the laboratory test, the input layer have 4 nodes which corresponding to the four variables of the cement materials, namely the concentration, fly ash, quicklime and cement, while the output layer has 5 nodes, which corresponding to slump, bleeding rate, compressive strength in age of 1d, 3d and 28d.

There is no explicit method to determine the number of nodes in the hidden layer so far, Such as Homik indicated the number of nodes in the hidden layer may between  $\sqrt{2m+1}$  and  $2m+n$ , Hecht Nielsen pointed out that the number is  $2m+1$ <sup>[8]</sup>, and another scholar raised the number is  $\sqrt{m+n}+a$ , in which  $a$  is a constant between 1 and 10<sup>[16]</sup>. In these methods,  $m$  and  $n$  are the number of nodes in the input layer and the output layer respectively. Therefore, the number of node in the hidden layer can be calculated as 3~13 based on the above empirical formulas. Taking the complex relationship between material performance and influence factors into account, the function *tansig* and *purelin* are selected as the transfer functions for hidden layer and output layer respectively.

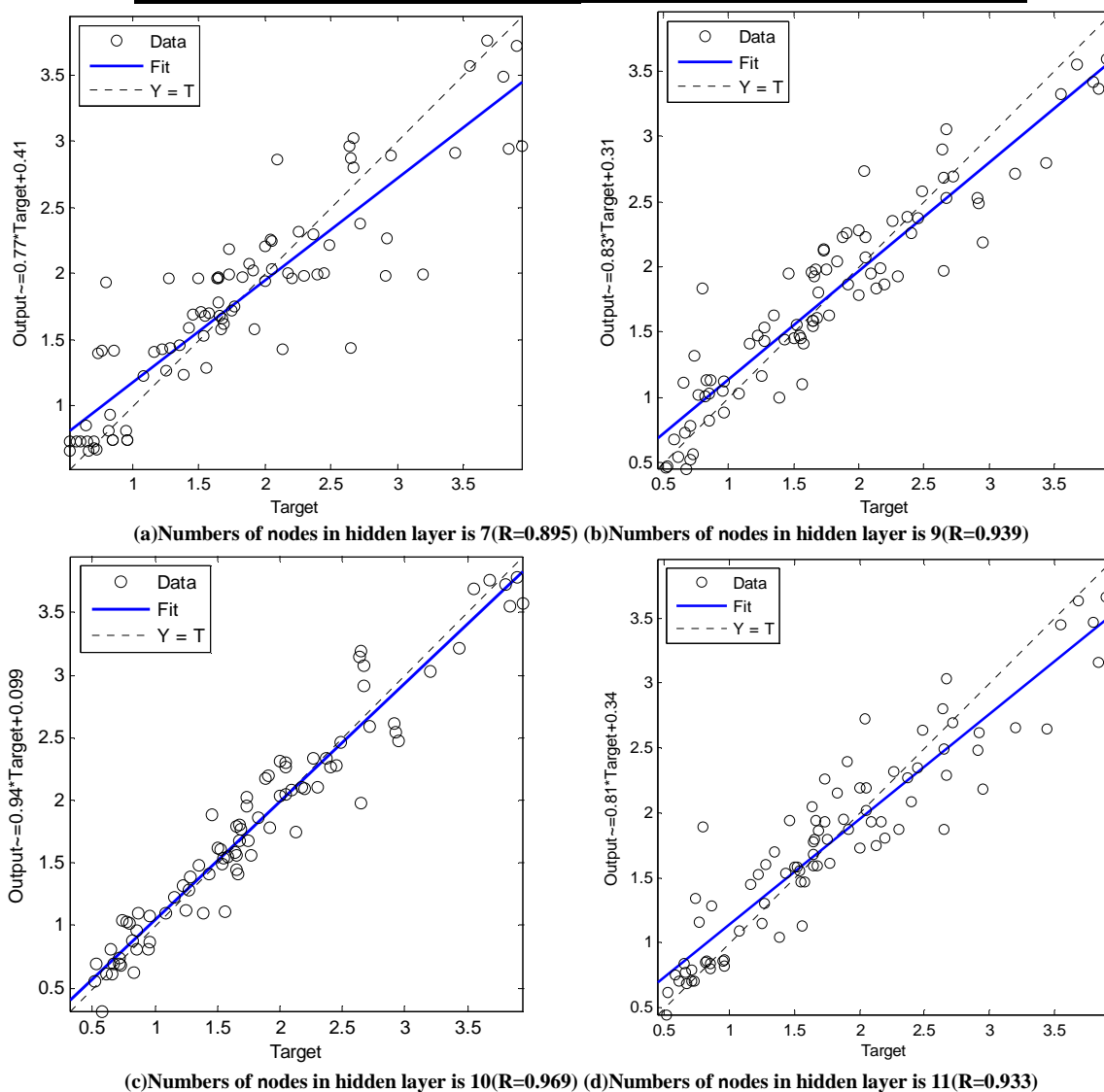
### 3.2 Training and prediction

The data of the first 17 groups from Tables 1 and Table 2 are selected as training samples, while the rest acted as test samples. *Training* self-adaptive learning algorithm is used to complete the network training and prediction, which was programmed and operated under Matlab 7.1 environment. The main parameters of the network are as follows: the target error is 0.0001, the maximum calculated numbers is 20,000, and the additional momentum factor is 0.90.

The typical training results are shown in Figure 2 for the training network with different numbers of nodes in the hidden layer, and the training error of network performance (MSE) and the fitting correlation coefficient of training results (R) are shown in Table 3.

**Tab.3 The performance of different numbers of nodes in the hidden layer**

Numbers of nodes in hidden layer	7	8	9	10	11	12	13
MSE	0.157	0.109	0.0871	0.0473	0.0834	0.0826	0.062
R	0.895	0.928	0.939	0.969	0.933	0.945	0.953



**Fig.2 Typical network training results**

As shown in Table 3, the hidden layer with 10 nodes has the best performance in training, and its training result and error curve are shown in Figure 2 (c) and Figure 3 respectively.

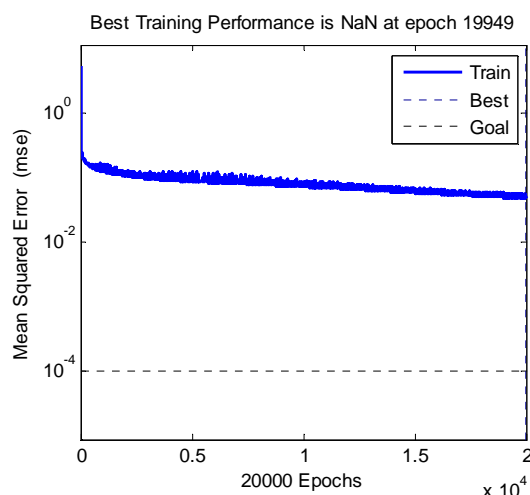


Fig.3 Curves of 10 nodes of hidden layer network training errors

As shown in Figure 3, there is still exist difference between the training errors and the target errors due to more nodes in the output layer and less data sample, and also the cemented filling material is a multiphase composite media, which exists uncertain factors during the performance test process.

The test sample was predicted using the trained network model with 10 nodes in the hidden layer and its results are shown in Table 4.

Tab.4 Test sample predictions

No. of ratio		18	19	20
Slump/mm	Measured value	247	165	150
	Predicted value	233	173	156
	error/%	5.67	4.85	4.00
Bleeding rate/%	Measured value	3.86	2.41	1.84
	Predicted value	3.74	2.20	1.92
	error/%	3.11	8.71	4.35
compressive strength of 3d /MPa	Measured value	0.65	0.62	1.05
	Predicted value	0.68	0.57	1.05
	error/%	4.62	8.06	0
compressive strength of 7d /MPa	Measured value	0.98	1.39	2.27
	Predicted value	1.09	1.50	2.00
	error/%	11.22	7.91	11.89
compressive strength of 28d /MPa	Measured value	1.46	1.74	3.33
	Predicted value	1.52	1.86	3.04
	error/%	4.11	6.90	8.71

As shown in Table 4, the error of predicting the performance of cement filling material by using the network model ranges between 0 to 11.89%, while the average error of 6.27%. Those results indicate that the performance prediction model of cemented filling material, based on the improved BPNN, has high prediction precision and generalization ability, which can be used to guide the production practice.

#### 4 Engineering Applications

The cement backfilling mining technology is taken into application to mine the extremely thick seam under the aquifer in Gonggeyingzi coal mine which located in Chifeng, Inner Mongolia. The compressive strength of cemented filling material in 3d age requires not less than 0.6MPa due to this special mining technology and in order to control the damage of roof strata after mining, the strength in 28d age requires not less than 2.0MPa. Moreover, in order to ensure the pumpability of the slurry, the slump is not less than 150mm and the bleeding rate is not more than 3%.

The performance of cemented filling material with different proportions are predicted by using the above trained network model in this paper. Finally, the optimal proportion, which not only meet the performance requirements but also reduce the dosage of cement, is obtained as follows, fly ash:35% , quicklime:10% , cement :2% , and gangue :53%. The concentration of slurry is 77%. Moreover, the strength of the samples which got from field in 3, 7 and 28 age is 0.76Mpa, 1.62Mpa and 2.23Mpa respectively, and the slump is 176mm and the bleeding rate is 2.75%, which meets the requirements of engineering. It shows the prediction model is accurate and reliable. The field application is shown in figure 4.

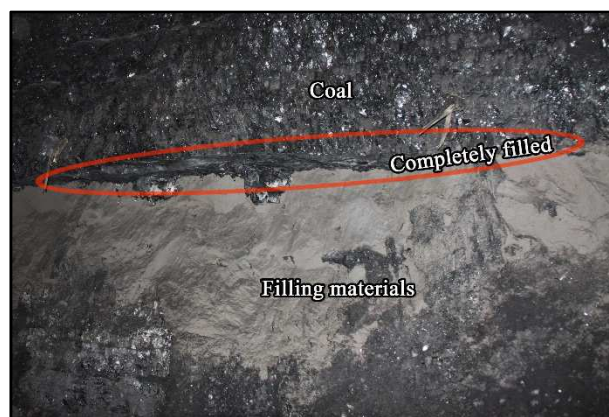


Fig.4 The field application

### CONCLUSION

- (1) The performance prediction model of the cemented filling material with 3 layers in which the hidden layer has 10 nodes was established based on improved BPNN in this paper. Through this model the complex mapping relationship between the performance of cemented filling materials such as the slump, the bleeding rate, the compressive strength in different ages and the ratio of the materials such as the concentration, the dosage of fly ash, quicklime, and cement is obtained to predict the performance of different ratio materials.
- (2) The self-adaptive learning rate arithmetic is adopted to train the network with the training and testing sample data collected from the laboratory test results, and the training results of MSE and R are 0.0473 and 0.969 respectively, which indicate a high precision. The prediction model was proved to meet the engineering requirements with the prediction error 0~11.89% , and the average 6.27% after testing the trained network model.
- (3) The well trained network model was applied to optimize the ratio of the cemented filling material in Gonggeyingzicool mine. Finally, the optimal proportion is obtained as follows, fly ash:35% , quicklime:10% , cement :2% , and gangue :53%. And the concentration of slurry is 77%. This ratio not only meets the requirements but also has low cost and good application effect.

### Acknowledgments

Financial support for this work provided by the Fundamental Research Funds for the Central Universities (No. 2013RC01), Project of National Scientific and Technical Supporting Programs Funded of China (No. 2012BAB13B03). Thanks for the scientific funding and industrial test site provided by Inner Mongolia Chifeng Silas Mulun Group. And thank the graduate students indeed for their contributions to this project, especially Zhou Nan, Zhang Qiang and Guo Shuai.

### REFERENCES:

- [1] Qian Minggao, Xu Jialin, Miao Xiexing. *Journal of China University of Mining & Technology*, **2003**(4):5-10.
- [2] Miao Xiexing, Qian Minggao. *Journal of Mining and Safety Engineering*, **2009**(1):1-14.
- [3] Qian Minggao, Miao Xiexing, Xu Jialin. *Journal of China Coal Society*, **2007**(1):1-7.
- [4] Zhou Huaqiang, Hou Chaojiong, Sun Xikui, et al. *Journal of China University of Mining & Technology*, **2004**(2):30-34+53.
- [5] He Rongjun, Zhang Li, Zhou Huaqiang, et al. *Journal of Mining and Safety Engineering*, **2008**(3):352-356.
- [6] Zhao Caizhi, Zhou Huaqiang, Bai Jianbiao, Qiang Hui. *Journal of Liaoning Technical University* (Natural Science Edition), **2006**, 06:904-906.
- [7] Chang Qingliang, Zhou Huaqiang, Qin Jianyun, et al. *Journal of Mining and Safety Engineering*, **2009**(1):74-77.
- [8] Wei Wei, Gao Qian. *Journal of Harbin Institute of Technology*, **2013**(6):90-95.
- [9] Zhao Caizhi, Zhou Huaqiang, Qu Qundi, et al. *Journal of China University of Mining & Technology*, **2004**(2):35-37.
- [10] Cui Zengdi, Sun Henghu. *Journal of China Coal Society*, **2010**(6):896-899.
- [11] Zhou Huaqiang, Hou Chaojiong, Wang Chenghuan. *Journal of China Coal Society*, **1992**(1):25-36.
- [12] Cui Mingyi, Sun Henghu. *Nonferrous Metals*, **2003**(1):121-123.
- [13] Cong Shuang. *Neural Network Theory And Applications with MATLAB Toolboxes* [M]. Hefei: University of Science and Technology of China Press, **2009**.
- [14] Zhang Qinli, Li Xieping, Yang Wei. *Journal of Central South University* (Natural Science Edition),

2013(7):2867-2874.

[15] Liu Zhixiang, Zhou Shilin. *Journal of Hunan University of Science & Technology* (Natural Science Edition), 2012(2):7-12.

[16] ZHENG Jingjing, ZHANG Qinli, WANG Xinmin, et al. *Journal of Xiangtan Normal University: Natural Science Edition*, 2008, 30(4): 40-44.