Fuzzy comprehensive evaluation and markov chain-based sports major teaching quality comprehensive evaluation research

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ABSTRACT

In order to improve sports teaching effects, the paper firstly carries out fuzzy qualitative and quantitative analysis of teaching quality evaluation indicator system’s numerous factors; divide teaching evaluation into learning attitude, learning method, learning ability, learning efficiency and faculty level five items evaluation factors. Apply fuzzy comprehensive evaluation principle and method. Construct sports teaching quality evaluation model, and transform it into centesimal system fraction. Use MATLAB to process with data, solve each class comprehensive score, finally on the basis of Markov chain, propose to construct transfer matrix on the basis of forward and post value state are consistent, and by proper handling, refine changing information from transfer matrix, and provide theoretical and practical evidence for reasonable, effective evaluate sports teaching effects.

Key words: Fuzzy comprehensive evaluation, teaching quality, membership, weight selection

INTRODUCTION

Presently regular institution of high learning sports learning effects evaluation contents mainly contain students theoretical knowledge, sports technology, physical quality and ordinary times performance, their occupied proportion are 10-15%, 30-60%, 10-20%, 10-20%. Theoretical attainment mainly investigates students selected course relative knowledge and so on, sports technology and physical quality mainly reference each school syllabus unified evaluation criterion, ordinary times performance refers to class attendance rate, attend class attitude is unified scored by teachers [1-6]. Presently universities current learning effects evaluation is unified, terminally teacher evaluation-led evaluation mode.

Current universities’ learning effects evaluation formulates unified criterion, target, encourages university students to positive take physical exercises, improve technology, brings students theoretical knowledge grasping into test results, which has larger improvements to a certain extent [7-10]. But it still has shortages. Evaluation contents are not comprehensive. Presently used evaluation lacks of evaluation on students’ learning process progress range, non-intellectual factors and other contents, is short of stimulation and guidance. It partially recognizes evaluation purposes. Unified criterion, summative evaluation only focuses on evaluation collection consulting, diagnosis of feedback purpose, it ignores that evaluation also has stimulation, guidance and cultivation self recognition functions. Evaluation, not only should summarize past, but also should be able to analyze present status and look forward the future. Evaluation subject is single, subjectivity is stronger, and it cannot scientifically make quantitative analysis. Evaluation mode that takes teachers evaluation as unique criterion is prone to cause errors in evaluation, is hard to be convinced by students, and difficult to play stimulating roles [11, 12].

Wang Yan, Zhou Hong(2006)pointed out present sport teaching evaluation methods selection was not scientific enough, evaluation criterion was too simple, which should select proper evaluation method according to concrete evaluation purposes and contents as other concrete status [1]. Ni Jian-Yin(2012)researched on junior high school
sports classroom teaching evaluation methods, research showed practice-based research could more scientific promote students sports and health level [2]. The paper applies fuzzy comprehensive evaluation principle and method, constructed sports teaching quality evaluation model.

FUZZY COMPREHENSIVE EVALUATION MODELS
In order to wholly understand students’ learning status, the paper references each education thesis to define evaluation factors, divides it into learning attitude, learning method, learning ability, learning efficiency and faculty level five items, and divides into twenty factors to make questionnaire survey, questionnaire statistics is as following Table 1.

Table 1: Questionnaire statistical table

<table>
<thead>
<tr>
<th>Evaluation element</th>
<th>Evaluation factor</th>
<th>Excellent (good)</th>
<th>Good (normal)</th>
<th>Medium (bad)</th>
<th>Bad</th>
</tr>
</thead>
<tbody>
<tr>
<td>F1 Learning attitude</td>
<td>1</td>
<td>371</td>
<td>367</td>
<td>75</td>
<td></td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>600</td>
<td>153</td>
<td>60</td>
<td>13</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>243</td>
<td>403</td>
<td>98</td>
<td>66</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>346</td>
<td>256</td>
<td>183</td>
<td></td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>259</td>
<td>453</td>
<td>102</td>
<td></td>
</tr>
<tr>
<td></td>
<td>6</td>
<td>423</td>
<td>272</td>
<td>106</td>
<td></td>
</tr>
<tr>
<td></td>
<td>7</td>
<td>502</td>
<td>137</td>
<td>156</td>
<td>24</td>
</tr>
<tr>
<td></td>
<td>8</td>
<td>359</td>
<td>329</td>
<td>105</td>
<td>29</td>
</tr>
<tr>
<td></td>
<td>9</td>
<td>600</td>
<td>153</td>
<td>60</td>
<td>14</td>
</tr>
<tr>
<td>F2 Learning method</td>
<td>10</td>
<td>503</td>
<td>258</td>
<td>43</td>
<td></td>
</tr>
<tr>
<td></td>
<td>11</td>
<td>274</td>
<td>444</td>
<td>78</td>
<td></td>
</tr>
<tr>
<td></td>
<td>12</td>
<td>420</td>
<td>257</td>
<td>139</td>
<td></td>
</tr>
<tr>
<td></td>
<td>13</td>
<td>502</td>
<td>259</td>
<td>43</td>
<td></td>
</tr>
<tr>
<td></td>
<td>14</td>
<td>264</td>
<td>444</td>
<td>88</td>
<td></td>
</tr>
<tr>
<td>F3 Learning ability</td>
<td>15</td>
<td>300</td>
<td>153</td>
<td>357</td>
<td></td>
</tr>
<tr>
<td></td>
<td>16</td>
<td>502</td>
<td>259</td>
<td>43</td>
<td></td>
</tr>
<tr>
<td></td>
<td>17</td>
<td>264</td>
<td>444</td>
<td>88</td>
<td></td>
</tr>
<tr>
<td></td>
<td>18</td>
<td>229</td>
<td>498</td>
<td>85</td>
<td></td>
</tr>
<tr>
<td>F4 Learning efficiency</td>
<td>19</td>
<td>744</td>
<td>53</td>
<td>8</td>
<td></td>
</tr>
<tr>
<td></td>
<td>20</td>
<td>174</td>
<td>382</td>
<td>180</td>
<td></td>
</tr>
<tr>
<td></td>
<td>21</td>
<td>564</td>
<td>122</td>
<td>11</td>
<td></td>
</tr>
<tr>
<td></td>
<td>22</td>
<td>286</td>
<td>422</td>
<td>61</td>
<td></td>
</tr>
</tbody>
</table>

Evaluation grade (remark) defining
In the questionnaire table, each evaluation factor has three or four options, to three options, on a whole, we can use qualitative description method to describe evaluation grade as: Good, normal, bad. Transfer it into quantitative description, then evaluation grade can be divided into 1 points, 0.7 points, 0.4 points that is \( v_j = (1, 0.7, 0.4) \). For four options’ topic, on a whole, we can use qualitative description method to describe evaluation grade as: excellent, good, medium, bad. And transfer them into quantitative description, then evaluation grade can be divided into 1 points, 0.8 points, 0.6 points, 0.4 points that is \( v_j = (1, 0.8, 0.6, 0.4) \).

Calculate evaluation factor membership \( A_{ij} \):

\[
A_{ij} = \frac{\sum_{i=1}^{12} A_{ij}}{\sum_{i=1}^{12} \sum_{j=1}^{5} A_{ij}}
\]

For example: The first factor, sports fondness level selection, there are totally 371 people love sports. And there are totally 367 people generally like sports; while totally 75 people dislike sports. Input data and can solve:

\[
A_1 = \begin{bmatrix}
371 & 367 & 75 \\
371+367+75 & 371+367+75 & 371+367+75 \\
\end{bmatrix}
\]

That is: \( A_1 = [0.5038, 0.4250, 0.0667] \).

Similarly it can solve each evaluation grade membership matrix \( A \).
Define each evaluation indicator weight

There are many methods to define evaluation indicator weights; it mainly has Delphi method, panel of experts consulting method, questionnaire survey, and analytic hierarchy process and so on. Reference above method can define each topic impacts on evaluation factor $T_i$, define its weights as $W_i$, for example impacts on learning attitude $T_1$, it can endow 1, 10, 15, 16, 19 weights as $W_1=(0.1 \ 0.2 \ 0.2 \ 0.3 \ 0.2)$

Solve fuzzy relation matrix

$$T_i = w_i \cdot B_j = (0.1 \ 0.2 \ 0.2 \ 0.3 \ 0.2) \cdot \begin{bmatrix} 0.8325 \\ 0.9388 \\ 0.8212 \\ 0.9124 \\ 0.8081 \\ 0.9974 \\ 0.8107 \\ 0.964 \\ \vdots \end{bmatrix} = \begin{bmatrix} 0.7207 \\ 0.7562 \\ 0.7675 \end{bmatrix}.$$

Learning attitude fuzzy relation matrix $T_1$:

Similarly it can solve that learning method is: 0.8673, learning ability is: 0.8409, learning efficiency is: 0.8094, faculty level is: 0.9067. Therefore, it is clear that the department students’ learning attitude is relative poor, faculty level is better, teachers mostly could do the due diligence themselves. It furthermore can solve students’ overall level comprehensive score:
In the following, we can also transform a group of fuzzy evaluation into quantity scores---centesimal system score is: \(0.8414 \times 100 = 84.14\) points.

To sum up, the department students are wholly good, comprehensive score is 84.14.

**MARKOV CHAIN MODEL**

Markov chain is a mathematical model that establishes on the random process. Due to in sports teaching evaluation field, numerous evaluation objects forming process can be regarded as or approximately regarded as random process, together with evaluators’ demands of understanding evaluation objects future value status, it let Markov chain to be widely applied in sports teaching evaluation.

Advantage of applying Markov chain method into sports teaching evaluation is considering that evaluation should eliminate basis differences. For example when evaluate different teachers’ teaching effects, it tends to give evaluation based on teachers’ lectured students’ final performance. In fact, different teachers’ lectured class students’ differences in original levels affect students’ final test performance. If simply evaluate teachers’ teaching effects according to students’ final performances without considering students’ basic differences’ affects, obtained conclusion cannot surely reflect practical situations, and the result is hard to be convincing. Thereupon, Markov chain analysis method considers students’ original state, under the same criterion, divides students’ original performance into same grade that is to define state space, and then solves one step transfer matrix, finally according to Markov chain stationary and periodicity, it solves extreme vector, and makes comparison and judgment according to extreme vector.

**Markov chain basic thought**

Markov chain application in sports teaching evaluation is on the basis of twice testing that is “Pre-test and post-test designing”, through carefully analyzing students’ twice testing changes in different performance grades, it constructs transfer matrix. On the condition that assume teaching efficiency remains steady, obtained Markov chain steady distribution state can show students’ final achieved extent. Concrete thought is as following:

In teaching efficiency indicator quantization process, apply Markov chain to respectively classify a class (or grade) students’ original performance according to high-low into \(q\) pieces of grades, and then calculate each grade students’ numbers to total numbers ratio as state vector, use \(A\) to express:

\[
A = \begin{pmatrix}
\frac{n_1}{n} & \frac{n_2}{n} & \cdots & \frac{n_q}{n}
\end{pmatrix}
\]

Among them, \(n\) is students total number, \(n_i\) is the \(i\) (\(i=1, 2, \cdots, q\)) grade number of people.

After several stages’ teaching, in order to investigate teaching efficiency, it needs to analyze above each grade students’ changing status after stage teaching, similarly also classify students’ performance tested after stage teaching according to high-low into \(q\) pieces of grades, count each grade contained students’ frequency, and further solve as next step transfer matrix \(P\):

\[
P = \begin{pmatrix}
\frac{n_{11}}{n_1} & \frac{n_{12}}{n_1} & \cdots & \frac{n_{1q}}{n_1} \\
\frac{n_{21}}{n_2} & \frac{n_{22}}{n_2} & \cdots & \frac{n_{2q}}{n_2} \\
\vdots & \vdots & \ddots & \vdots \\
\frac{n_{q1}}{n_q} & \frac{n_{q2}}{n_q} & \cdots & \frac{n_{qq}}{n_q}
\end{pmatrix}
= \left(\begin{pmatrix}
p_{ij}\end{pmatrix}\right)_{q \times q}
\]

Among them, \(n_i\) still represents preliminary stage the \(i\) grade students amount, \(n_{ij}\) represents after stage teaching, affiliated to the \(i\) grade students performances belong to the \(j\) kind students amount, and
\[ \sum_{j=1}^{q} P_{ij} = 1, \quad 0 \leq P_{ij} \leq 1 \quad (i, j = 1, 2, \cdots, q) \]

If to research multiple steps \((k > 1)\) transition probability \(P^{(k)}\), utilize Chamman-Kolmogorov equation, it has:

\[ P^{(k)} = P^{(k-1)} P^{(1)} = \cdots = \left[ P^{(1)} \right]^k \]

When \(k \sim \infty\), if Markov process involved each state probability distribution is steady and unchanged (the attribute is called periodicity, corresponding probability distribution is steady distribution), thereupon, it can solve steady probability vector, the steady and unchanged probability vector becomes evaluation criterion, and then get concrete quantitative indicator value by solving equation set.

**Model application**

(1) Value state consistency

In teaching practice, utilize Markov chain method to evaluate sports teaching, generally it applies successive two values states (as twice test results) connections to describe transition probability matrix, and accordingly make evaluation on evaluation object achieved current state practices. But whether successive twice used value scale is consistent or not, successive twice evaluation scenes of evaluation objects are consistent or not, both of them will affect defined state matrixes. Now take one class successive twice tests as examples, assume the first time the class test average result is 80 points, standard deviation is 10 points, and there are ten people in [100, 90] points, fifteen people in [90, 80] points, ten people in [80, 70] points, six people in [70, 60] points, four people in [60, 0] points. In the second time test, the class average result is 85 points, standard deviation is 8 points. And, the first time test result distribution in the second time test result is as Table 2:

<table>
<thead>
<tr>
<th>The first time test result</th>
<th>The second time test result</th>
</tr>
</thead>
<tbody>
<tr>
<td>100~90</td>
<td>8</td>
</tr>
<tr>
<td>90~80</td>
<td>2</td>
</tr>
<tr>
<td>80~70</td>
<td>3</td>
</tr>
<tr>
<td>70~60</td>
<td>2</td>
</tr>
<tr>
<td>60~0</td>
<td>2</td>
</tr>
</tbody>
</table>

Therefore established transition probability matrix is:

\[
\begin{pmatrix}
0.8 & 0.2 & 0 & 0 & 0 \\
0.2 & 0.8 & 0 & 0 & 0 \\
0 & 0.5 & 0.2 & 0.3 & 0 \\
0 & 0 & 0.5 & 0.5 & 0 \\
0 & 0 & 0 & 0.5 & 0.5
\end{pmatrix}
\]

On the other hand, if both transform twice test results into Z-standard score, then it can change Table 2 into Table 3:

<table>
<thead>
<tr>
<th>The first time test result</th>
<th>The second time test result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.88~0.63</td>
<td>8</td>
</tr>
<tr>
<td>0.63~0.63</td>
<td>2</td>
</tr>
<tr>
<td>-0.63~1.88</td>
<td>3</td>
</tr>
<tr>
<td>-1.88~3.22</td>
<td>12</td>
</tr>
<tr>
<td>-3.22~10.63</td>
<td>1</td>
</tr>
</tbody>
</table>

By above Table 3, it is clear that successive twice test scores are not equal, first time test result five states and second time test results five states have no comparability. Therefore, established transition probability matrix significances are unconvincing.
(2) Value state probability distribution

Markov chain described process is when $K$ tends to be infinitely great, appears or arrives at each state probability distribution is steady and unchanged, and then it can utilize Markov chain model to evaluate. When utilize obtained probability vector to solve equation set, it has already artificially defined vector feature root as 1, and further establish evaluation criterion. As for each state arrive at stable and unchanged or not, utilize should verify by solving, and in practical teaching application, evaluator don’t consider the condition but assume it arrives at steady state, in fact, the condition has certain effects on constructing steady probability distribution.

Model improvement

(1) Construct transition matrix

Combine students’ successive twice test results into a sample $(x_{11}, x_{12}, \cdots, x_{1m}, x_{21}, x_{22}, \cdots, x_{2m})$, solve its average number $(\bar{x})$ and standard deviation $(S)$. Due to research shows that students’ academic achievement basically is in normal distribution or gets closer to normal distribution, therefore according to normal distribution law, utilize $\bar{x}$ and $S$ to classify certain intervals’ $q$ pieces of grades. Then use $q$ pieces of grades to calculate students previous time test each grade students number occupied total number proportion’s state vector, use $A$ to express:

$$A = \left(\frac{n_1}{n}, \frac{n_2}{n}, \cdots, \frac{n_q}{n}\right)$$

Among them, $n$ is students total number, $n_i$ is the $i$ grade number of people.

In order to investigate teaching effects, it needs to analyze above each grade students each grade changing status in the second time test. Similarly also according to $q$ pieces of grades interval criterion, count second time test result each grade contained students’ frequency, and further solve as following one step transition matrix $P$:

$$P = \begin{pmatrix}
\frac{n_{11}}{n_1} & \frac{n_{12}}{n_1} & \cdots & \frac{n_{1q}}{n_1} \\
\frac{n_{21}}{n_2} & \frac{n_{22}}{n_2} & \cdots & \frac{n_{2q}}{n_2} \\
\vdots & \vdots & \ddots & \vdots \\
\frac{n_{q1}}{n_q} & \frac{n_{q2}}{n_q} & \cdots & \frac{n_{qq}}{n_q}
\end{pmatrix} = (P_{ij})_{q \times q}$$

Among them, $n_i$ still represents the preliminary stage the $i$ grade students number, $n_{ij}$ represents after stage teaching, affiliated to $i$ grade students performance that belong to $j$ kind students number, and meet $\sum_{j=1}^{q} p_{ij} = 1$, $0 \leq P_{ij} \leq 1$, $(i, j = 1, 2, \cdots, q)$. In this way it solves value states inconsistency problems, and fully gives Markov chain one step transition matrix features into play, that is to say, it can eliminate basic differences, and also can concentrate on reflecting its changing efficiency advantage.

(2) Establish model and analysis

In order to avoid Markov chain occurring multiple steps transition, and is required to solve steady probability distribution on the condition of extreme state such rigor condition. After considering one step transition matrix, utilize students’ “progress degree” that students make progress or retrogress such problems, which is to concern a class or a grade students’ performance is as progress is larger than retrogress, or retrogress is larger than progress, to grasp the overall progress status. Now assume that cultivate $i$ grade students into $j(i > j)$ grade students is progress, cultivate $i$ grade students into $j(i < j)$ grade students is retrogress, grasp the point then it can eliminate basic difference, and meanwhile can also reflect teaching efficiency merits. In order to correctly refine changing information from transition matrix, specially establish following model:

$$S_{ij} = (i - j) \frac{n_i}{n}, (i, j = 1, 2, \cdots, q).$$

Among them, $S_{ij}$ is called $P_{ij}$ transferring progress degree,
\((i-j)^2\) is called \(p_{ij}^2\) weight. \(i-j\) value size and positive or negative represents progress or retrogress extent, index “3” is used to adjust positive or negative and weight sizes.

\[
S = (S_{ij})_{q \times q} = \frac{(i-j)^3 n_j}{n_i}
\]

is called transition matrix \(P_{ij}\) progress matrix.

\[
E_\text{(s)} = \sum_{i=1}^{q} \sum_{j=1}^{q} (i-j) p_{ij}^3 = \sum_{i=1}^{q} \sum_{j=1}^{q} (i-j) \frac{n_j}{n_i}
\]

is called transition matrix \(P_{ij}\) efficiency degree.

**Model comparison**

Now assume that its test used value scale is consistent. In the end of first school year, two classes sports comprehensive test each grade state vector (excellent, good, medium, qualified, unqualified):

\[
C_A = \left(\begin{array}{ccccc}
46 & 23 & 7 & 1 & 0 \\
46 & 23 & 7 & 8 & 0 \\
46 & 23 & 7 & 4 & 0 \\
46 & 23 & 7 & 3 & 0 \\
46 & 23 & 7 & 2 & 0 \\
46 & 23 & 7 & 1 & 0 \\
46 & 23 & 7 & 0 & 0 \\
46 & 23 & 7 & 0 & 0 \\
46 & 23 & 7 & 0 & 0 \\
46 & 23 & 7 & 0 & 0 \\
\end{array}\right), \quad C_B = \left(\begin{array}{ccccc}
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
22 & 8 & 1 & 0 \\
\end{array}\right)
\]

After one year teaching, two class’s students’ sports state probability transition matrix:

\[
P_A = \left(\begin{array}{cccccc}
\frac{3}{8} & \frac{1}{8} & 0 & 0 & 0 \\
\frac{5}{23} & \frac{4}{23} & \frac{3}{23} & \frac{2}{23} & 0 \\
0 & \frac{3}{23} & 0 & 0 & 0 \\
0 & \frac{3}{7} & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
\end{array}\right), \quad P_B = \left(\begin{array}{cccccc}
\frac{2}{7} & \frac{3}{7} & \frac{1}{7} & \frac{1}{7} & 0 \\
\frac{11}{22} & \frac{3}{22} & \frac{1}{22} & \frac{1}{22} & 0 \\
0 & \frac{5}{22} & \frac{1}{22} & \frac{1}{22} & 0 \\
0 & \frac{5}{8} & \frac{1}{8} & \frac{1}{8} & 0 \\
0 & 0 & 0 & 0 & 0 \\
\end{array}\right)
\]

Set grade state vector (excellent, good, medium, qualified, unqualified) respectively to be replaced by (1, 2, 3, 4, 5, ), it can get \(P_A\) progress matrix is:

\[
S_A = \left(\begin{array}{cccccc}
0 & \frac{1}{4} & -1 & 0 & -12 \\
\frac{5}{23} & 0 & -\frac{4}{23} & \frac{32}{23} & 0 \\
0 & \frac{8}{7} & 0 & 0 & 0 \\
0 & \frac{8}{7} & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 \\
\end{array}\right), \quad S_B = \left(\begin{array}{cccccc}
0 & -\frac{3}{7} & \frac{8}{7} & -\frac{27}{7} & 0 \\
\frac{8}{22} & 0 & -\frac{3}{22} & -\frac{32}{22} & 0 \\
1 & \frac{3}{8} & 0 & 0 & 0 \\
0 & \frac{5}{8} & 0 & -\frac{1}{8} & 0 \\
0 & 0 & 0 & 1 & 0 \\
\end{array}\right)
\]

It can get: \(E(S_A) \approx -9.64\), \(E(S_B) \approx -3.79\). Therefore, it shows class B teaching efficiency is obvious better than class A. Only from improved Markov chain method, it can also see that two classes teaching efficiency is not so high, because in the view of model perceptual intuition, if teaching efficiency is high, then cultivate \(i\) grade students into \(j(i > j)\) grade students would be more, \(i-j\) value is positive, possibility that \(E_\text{(s)}\) to be positive would be large.

**CONCLUSION**

The paper through students’ reflection and evaluation, applies fuzzy mathematical theory to establish fuzzy comprehensive evaluation mathematical model. Established fuzzy comprehensive evaluation model not only well solves sports teaching quality evaluation problem, but also the model can be promoted and applied into other
evaluation models. Meanwhile used Markov chain considers transition matrix construction meanings, and fully utilizes Markov chain one step transition matrix basic features, correctly refines changing information from transition matrix without excessive assumption conditions, established model is simple, reasonable and practical, which has important significances in effective evaluating sports teaching effects.

REFERENCES